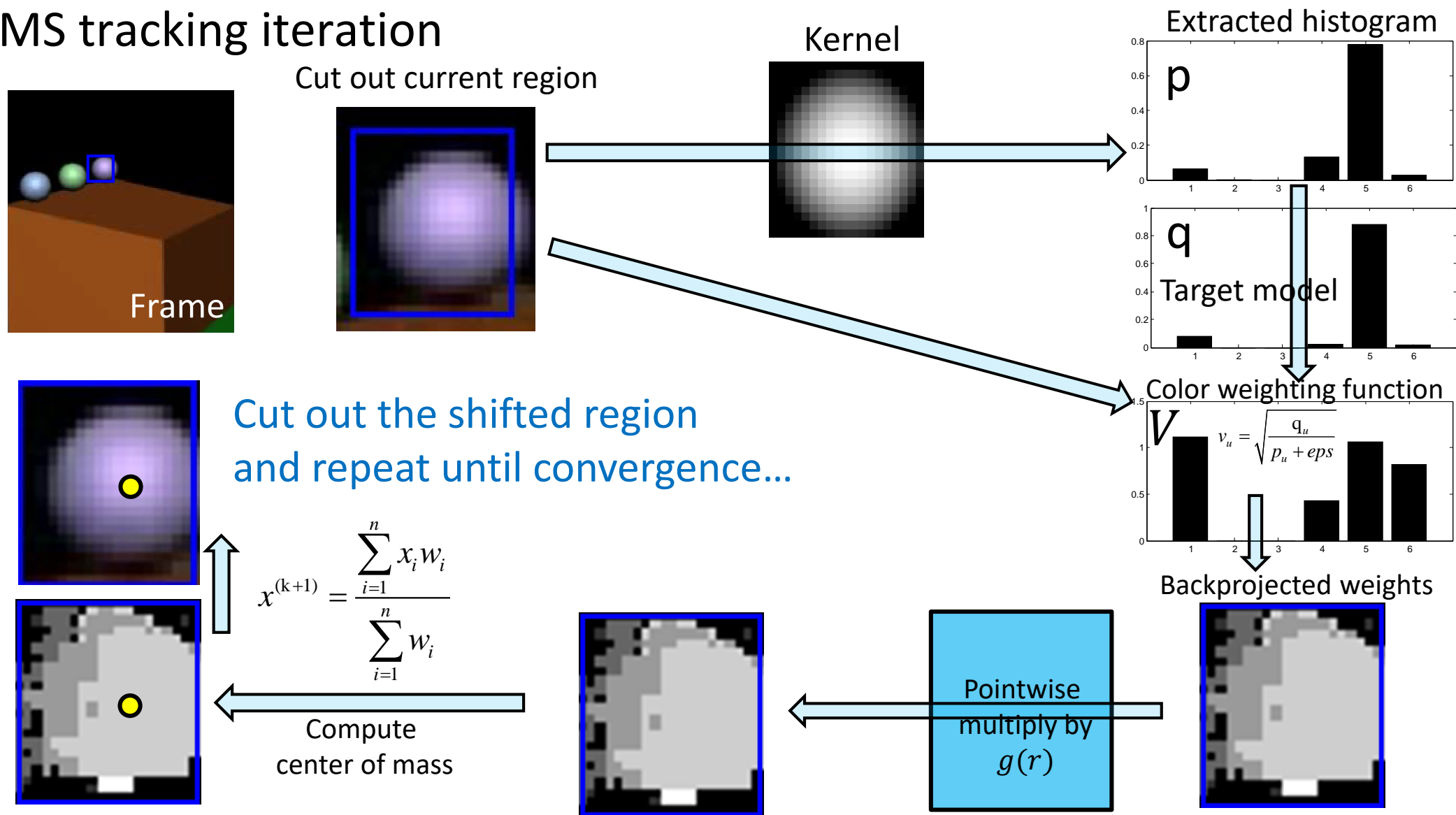


Previously at ACVM...

- MS tracking iteration





Advanced CV methods

Discriminative tracking – tracking by classifiers

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Fakulteta za računalništvo in informatiko,
Univerza v Ljubljani

Tracking by detection

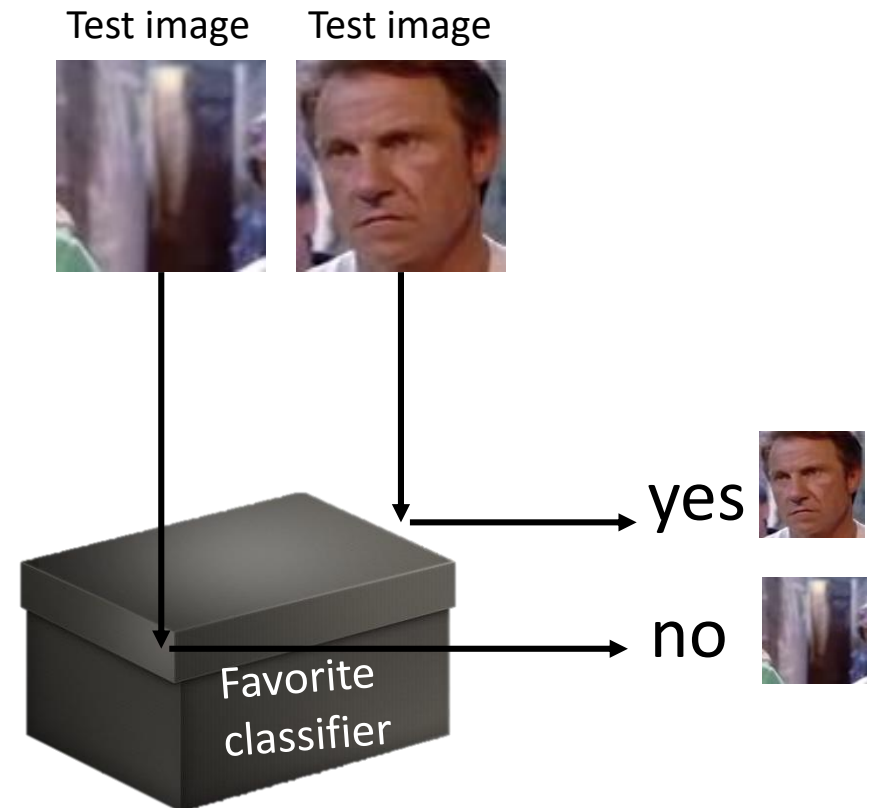
- A case study: tracking faces
- Take a (huge) number of cropped face image and even larger number of non-face images



Positive training examples

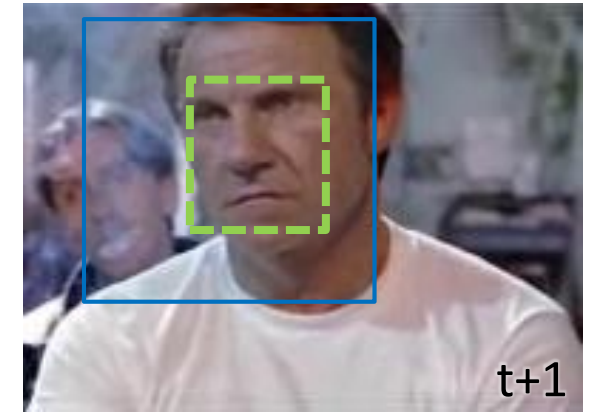
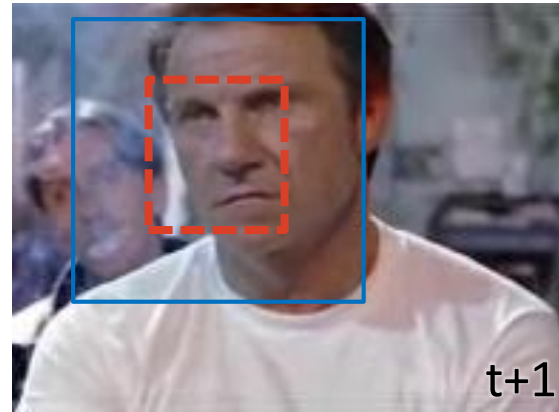
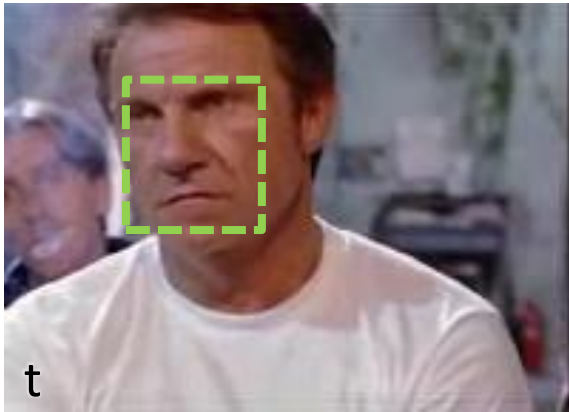


Negative training examples



Online discriminative tracking

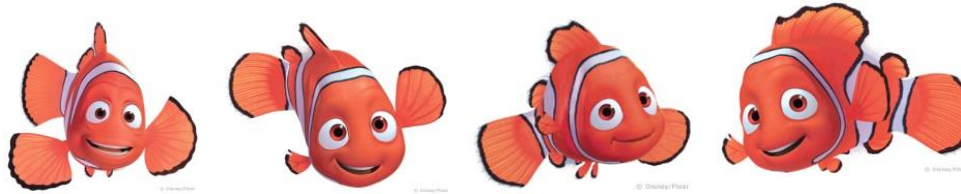
- The target **does not move a lot** between consecutive frames.
- Apply sliding window only within the region located at previous position.



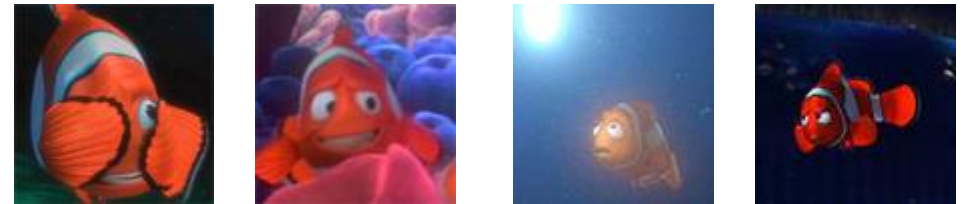
- Choice of the type of classifier (object model) crucial for practical purpose!

Requirements of object model

- Appearance model capability to adapt
 - Appearance changes (e.g. out of plane rotations)



- Appearance model robustness
 - Occlusions, cluttered background, illumination conditions

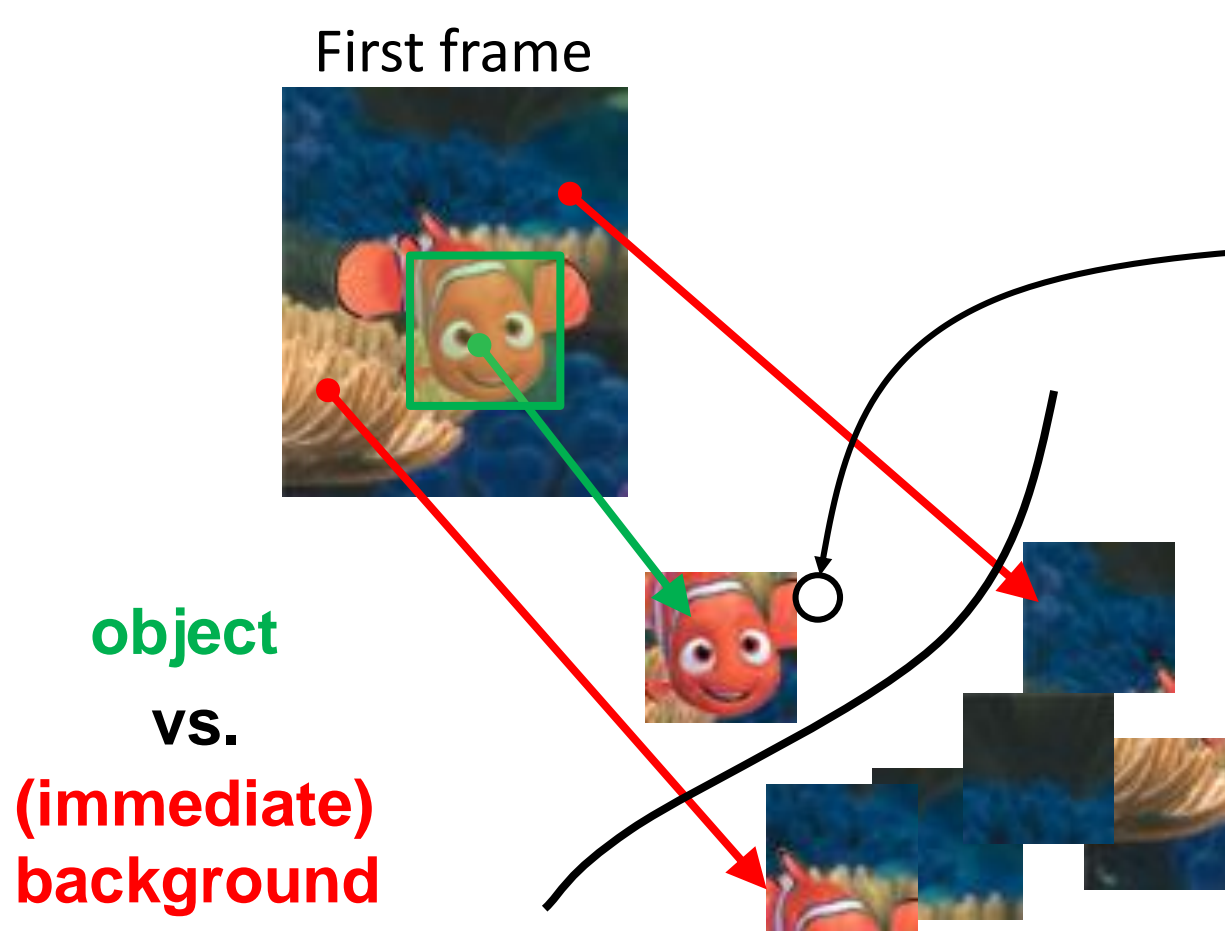


- Appearance model generality
 - Any object

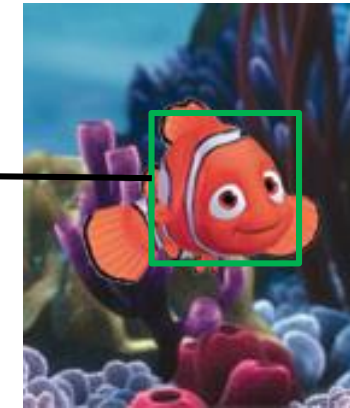


Tracking as a binary classification

- A **single supervised training example** provided in the first frame



Next frame




- But this **classifier might not be valid** any more for the next frame.
- **(Self-supervised) update** is required.

Tracking as a binary classification

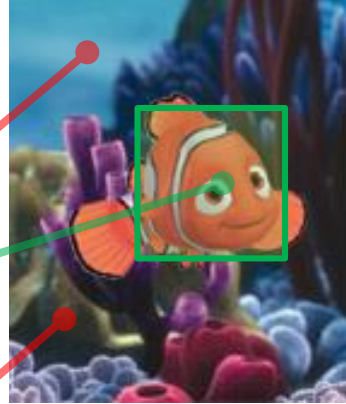
S. Avidan. **Ensemble tracking**. CVPR 2005.
J.Wang, et al. **Online selecting discriminative tracking features using particle filter**. CVPR 2005.

- A single supervised training example provided in the first frame

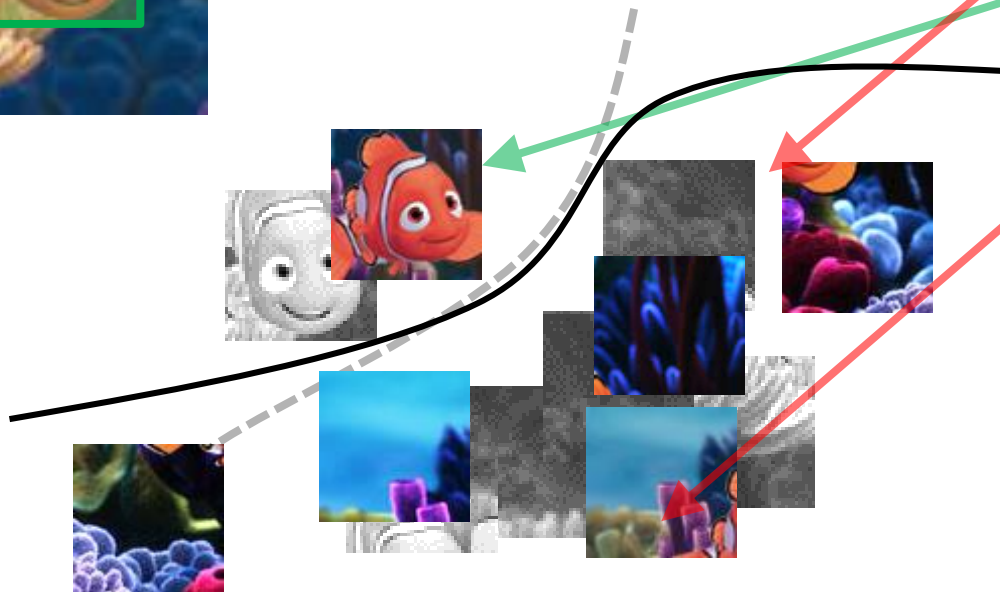
First frame



Next frame



object
VS.
(immediate)
background



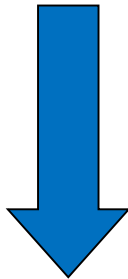
- Select positive examples from the target position.
- Select negative examples from the immediate background

Boosting for Feature Selection

Object Detector

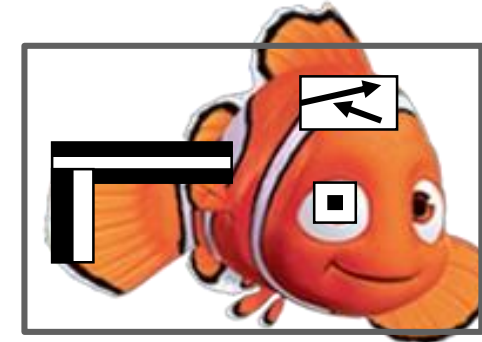
P. Viola and M. Jones. Rapid object detection using a boosted cascade of simple features. CVPR 2001.

Fixed Training set
General object
detector



Object Tracker

On-line update
Object vs. Background



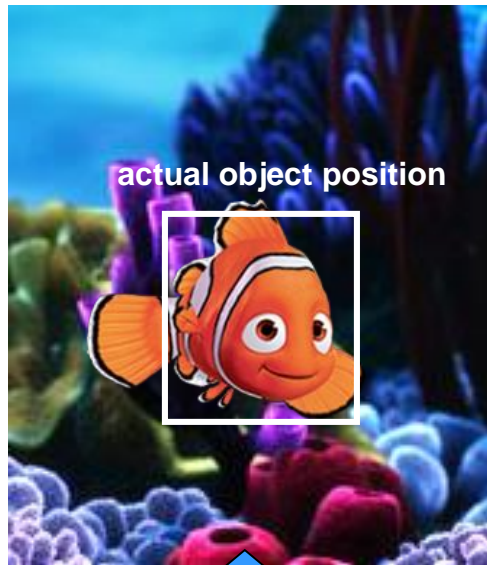
$$\text{sign}(\alpha_1 \cdot \text{feature}_1 + \alpha_2 \cdot \text{feature}_2 + \alpha_3 \cdot \text{feature}_3 + \dots)$$

Combination of simple image features
using Boosting as Feature Selection

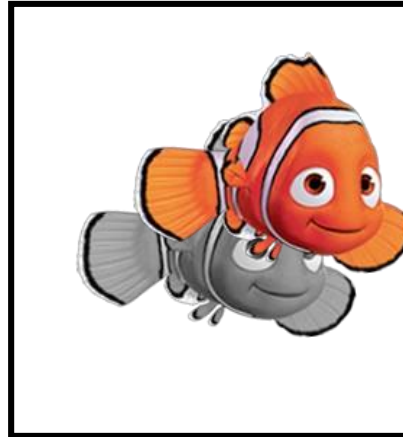
On-Line Boosting for Feature Selection

H. Grabner and H. Bischof. On-line boosting
and vision. CVPR, 2006.

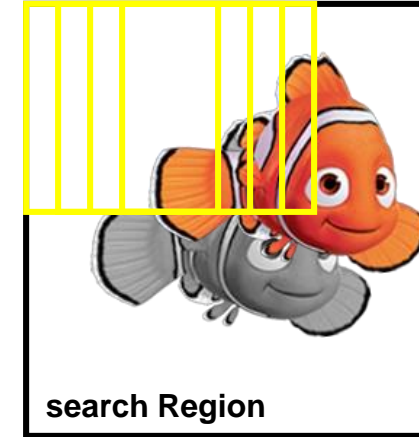
Tracking by online Adaboost



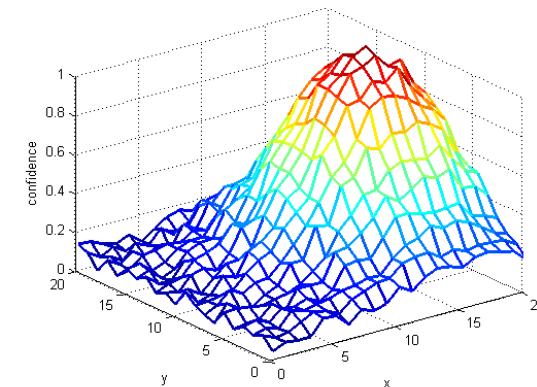
from time t to $t+1$



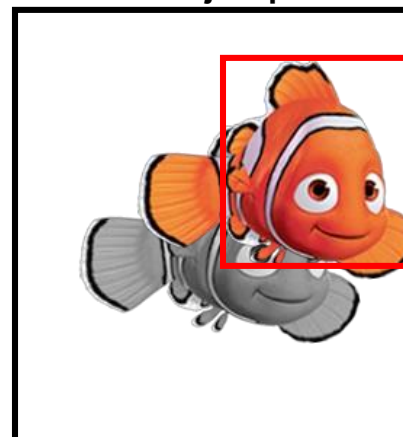
evaluate classifier on sub-patches



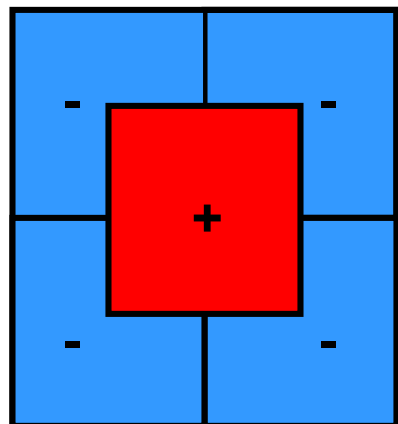
create confidence map



Select the maximum as the new object position



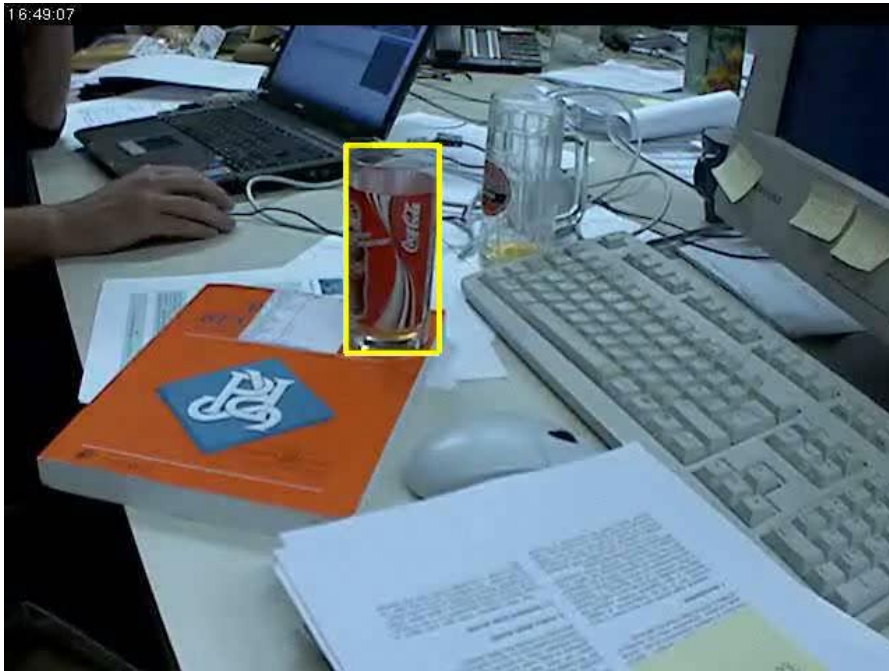
update classifier (tracker)



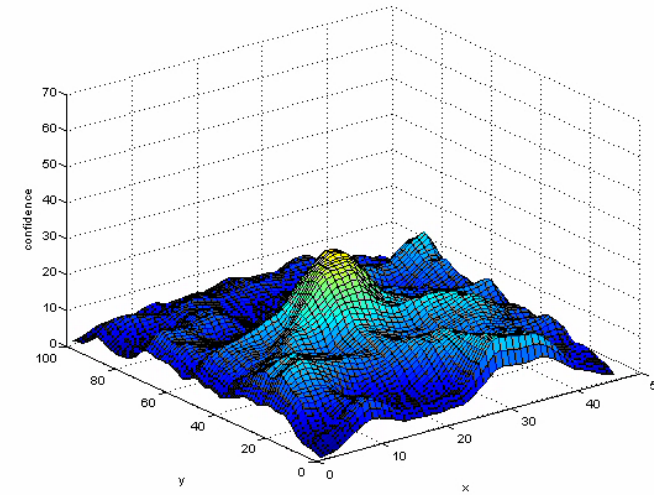
Tracking by online Adaboost

- Realtime performance
 - Fast feature computation
 - Efficient update of classifier

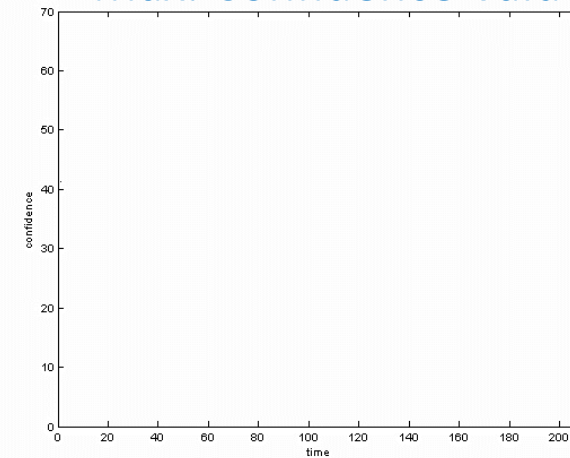
Tracking



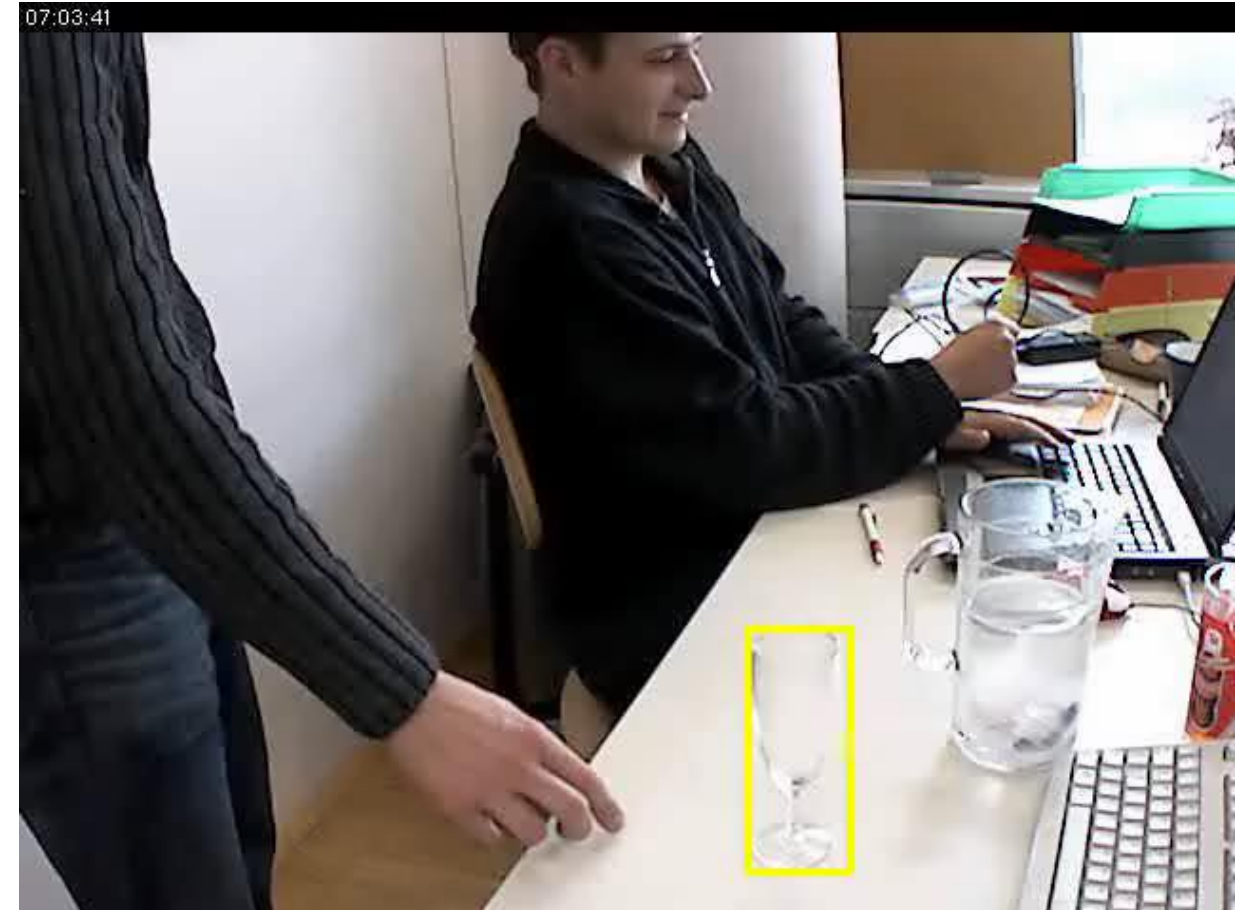
Confidence Map



Max. Confidence Value

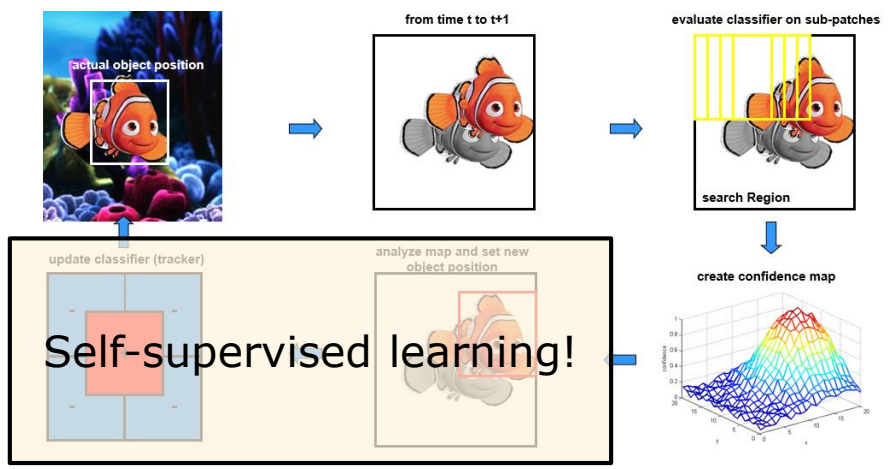
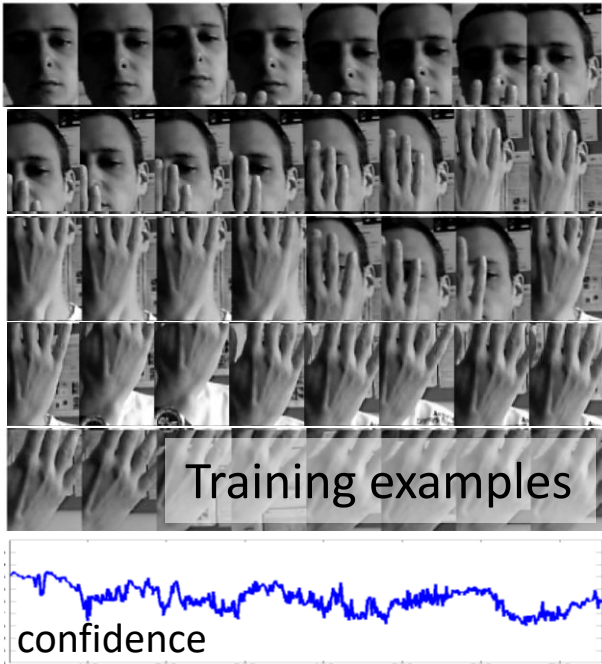
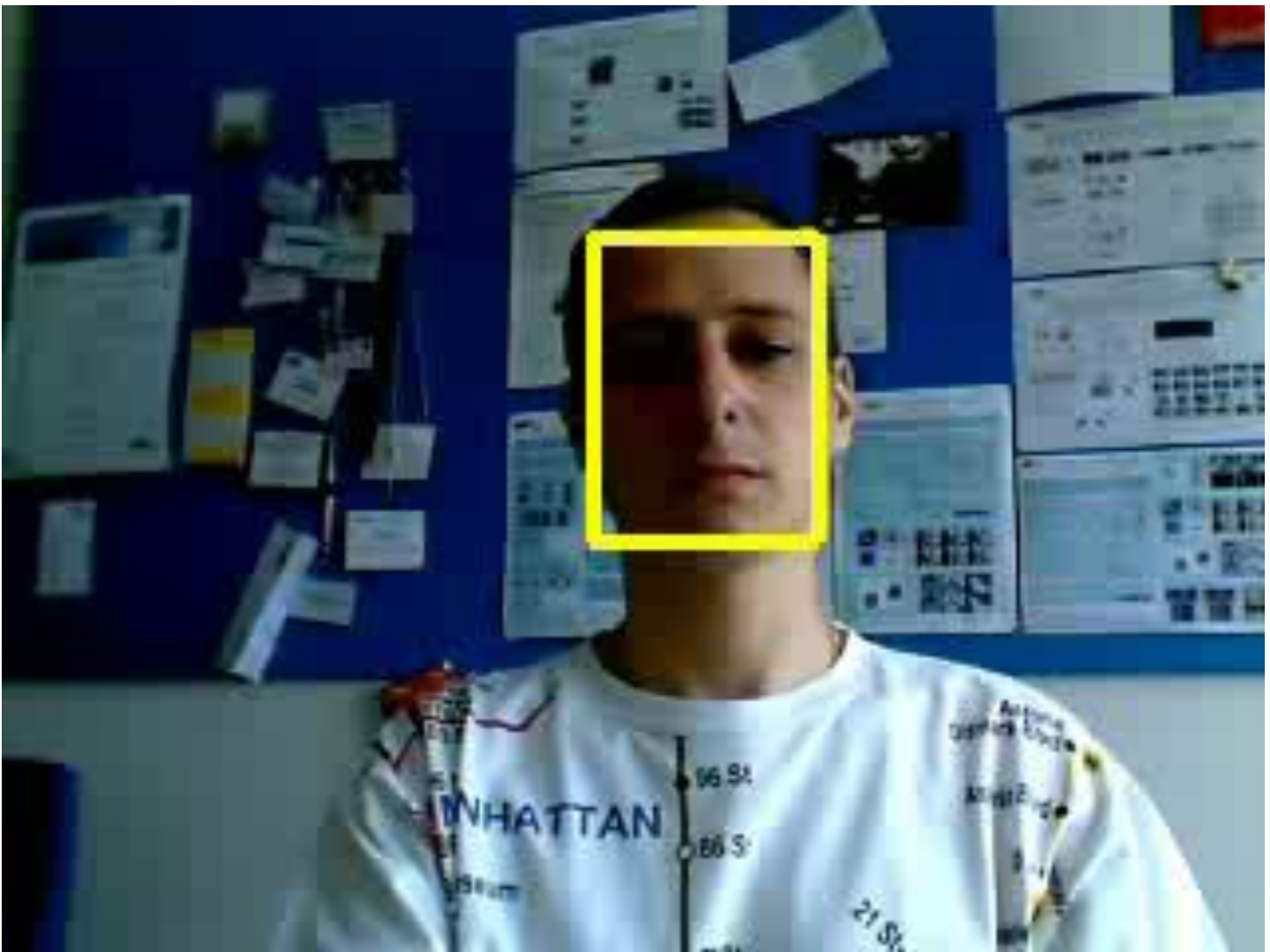


Tracking by online Adaboost

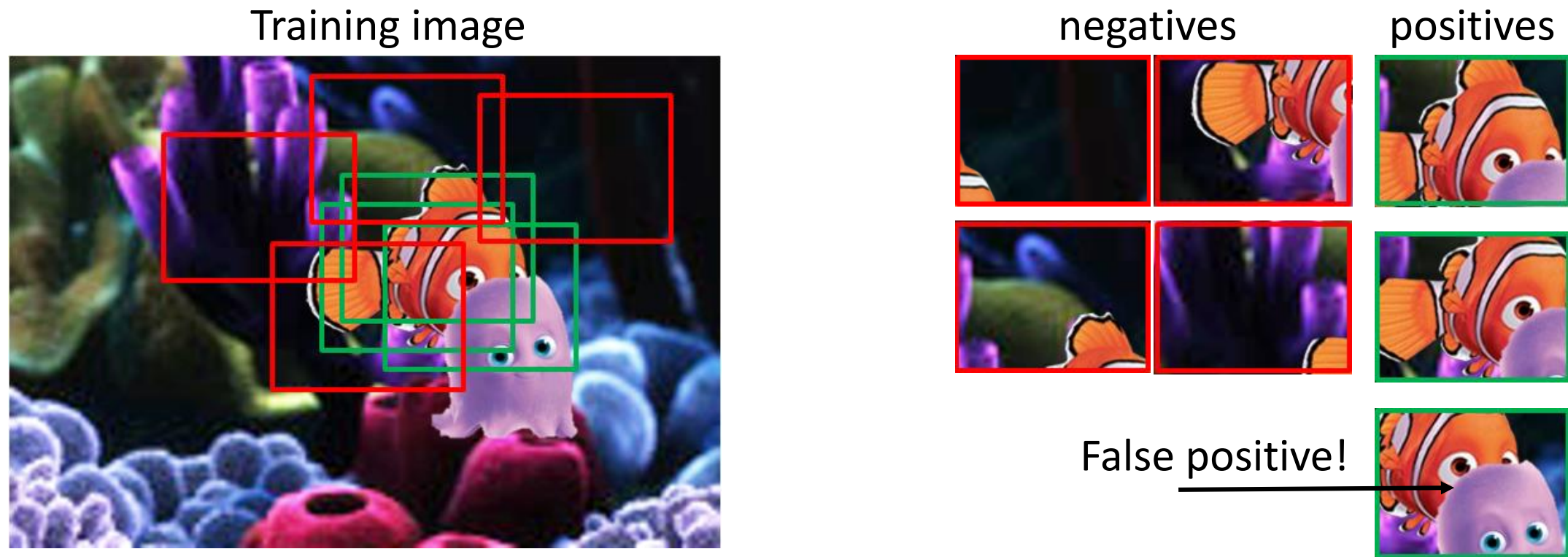


H. Grabner et. al., Real-Time Tracking via On-line Boosting . BMVC, 2006.

Failure modes

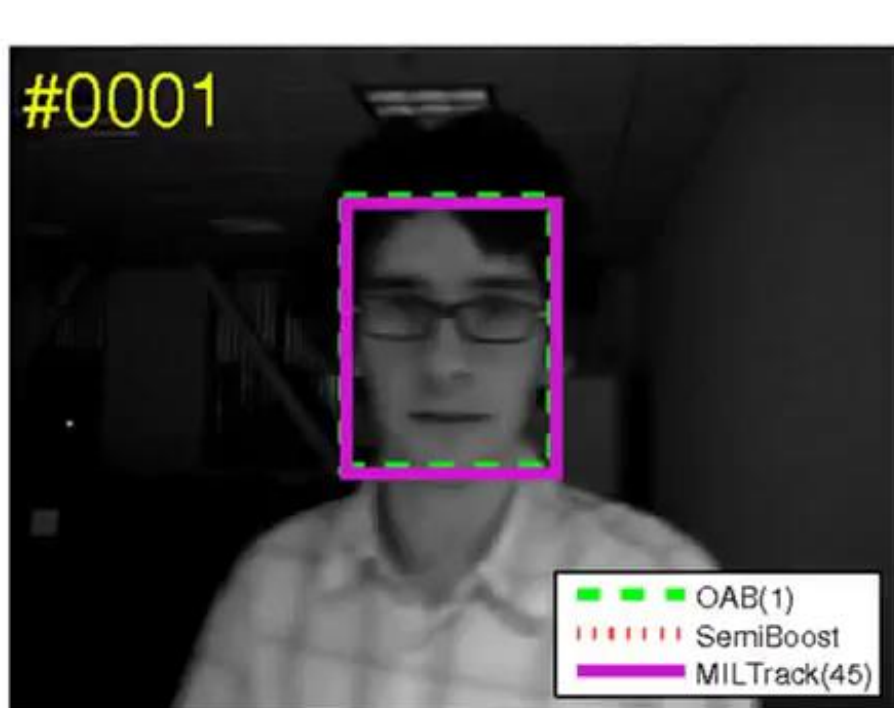


Do not trust all learning examples



- Assume **all negative examples** are **really negative**
- Assume **positive examples** might **contain some negatives**
- A multiple instance learning (MIL) problem!

Do not trust all learning examples

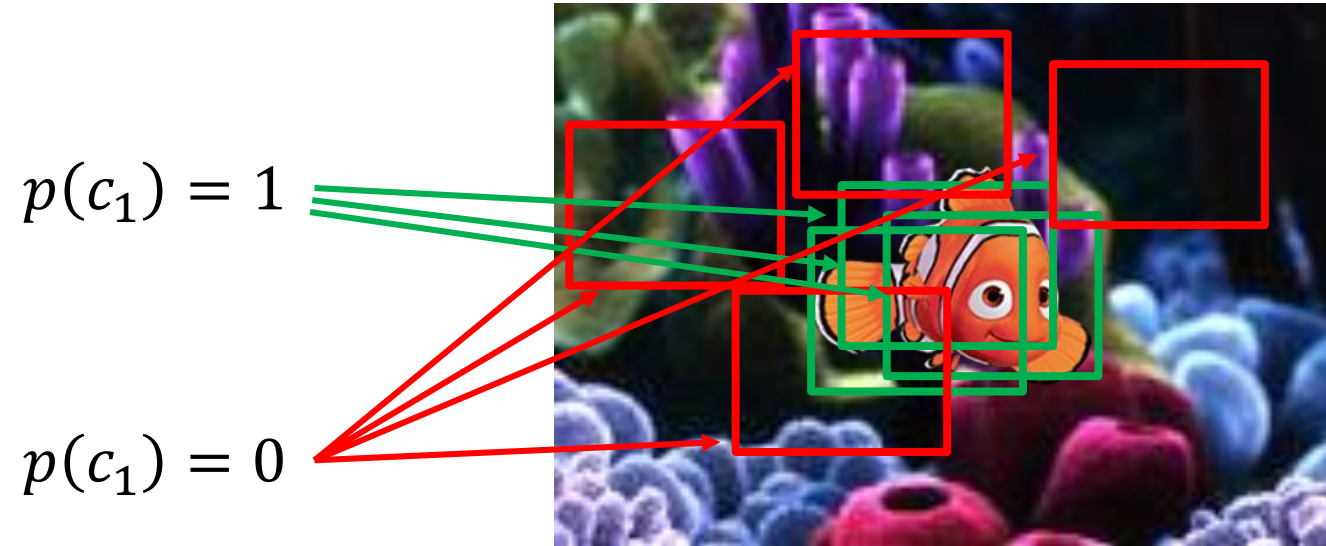


- Note that the [online Adaboost failed in this run](#) on the David sequence!
- Be sure that TMIL authors worked to show this, but it also [says a lot about robustness](#) of oAB to initialization!
- Code for TMIL available [here](#).

Babenko et al., "[Robust Object Tracking with Online Multiple Instance Learning](#)", TPAMI2011

Apply weights to training examples

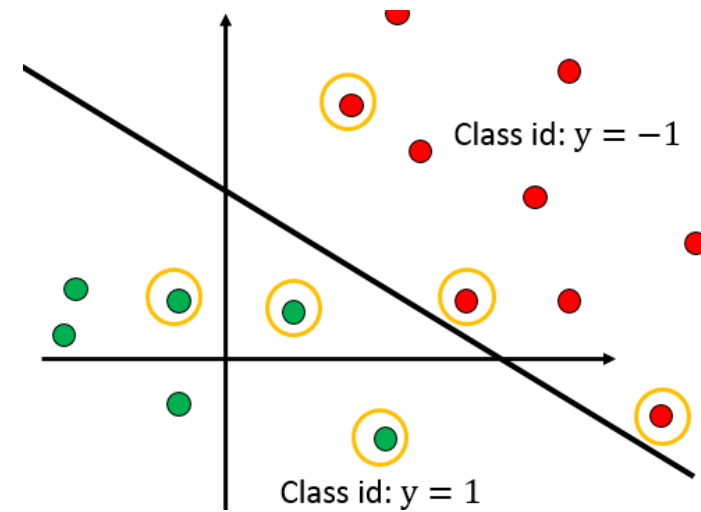
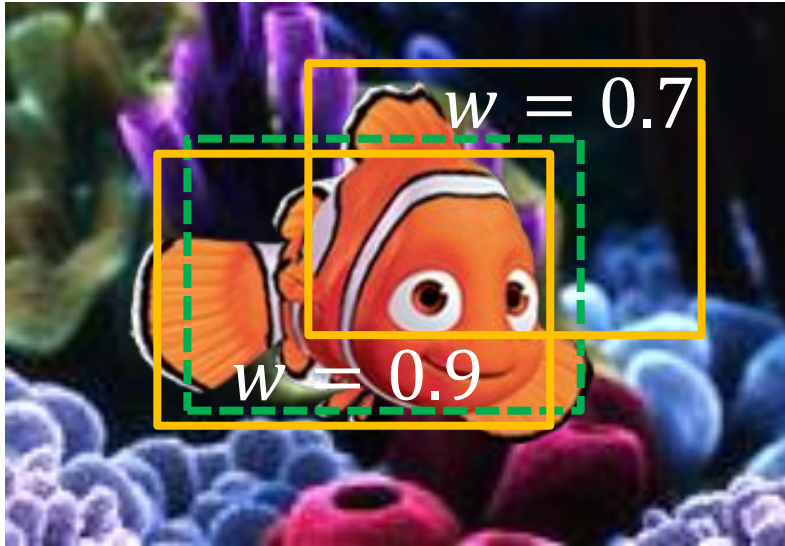
- Online AdaBoost and TMIL make hard decision on the class identity :



- But **some positive examples are more positive** than others and some negative examples are “more negative” than others...

Apply weights to training examples

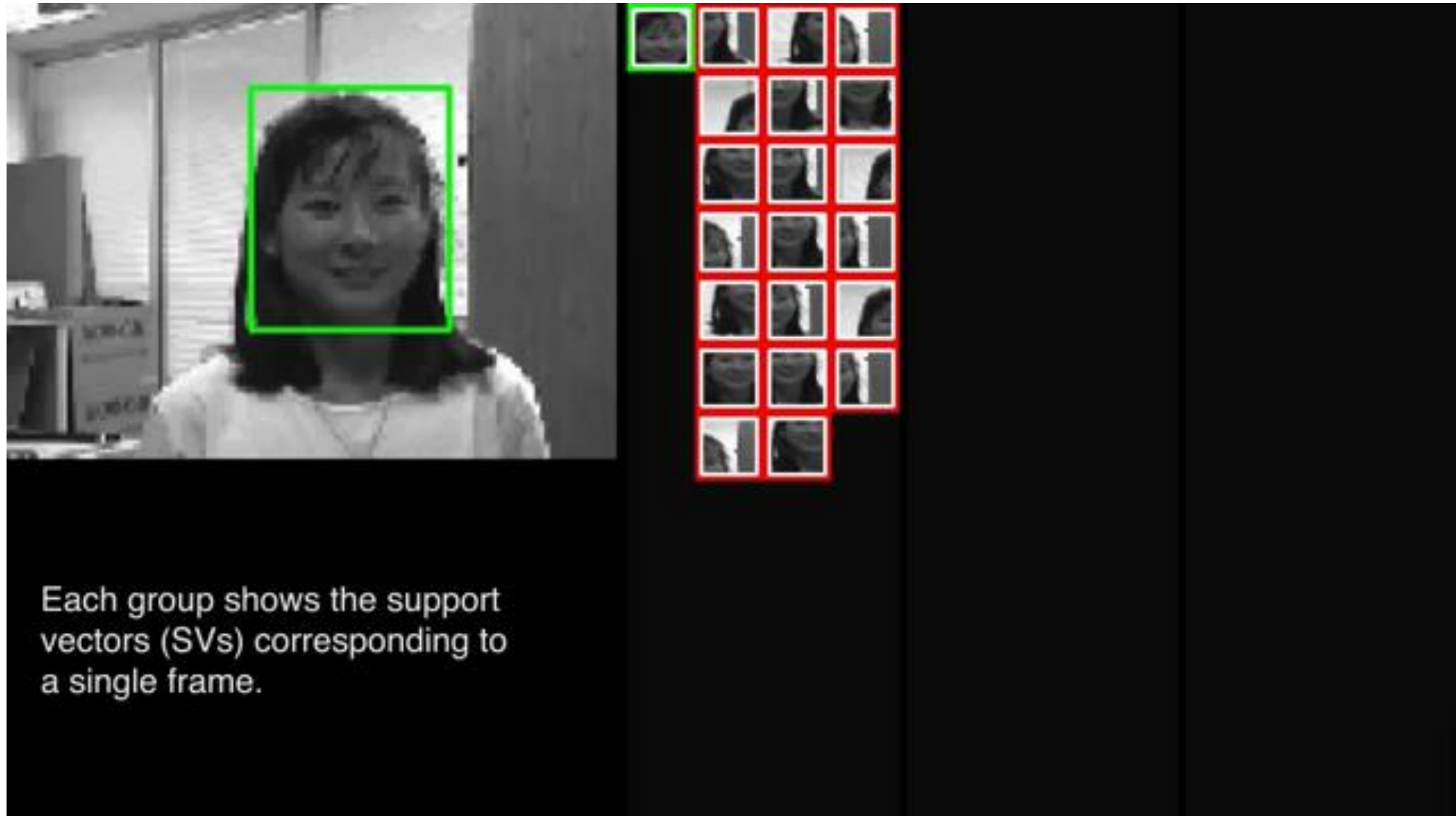
- Weights proportional to estimated position overlap:



- Learning machinery:
 - Structured Support Vector Machine (online version)

Sam Hare, Amir Saffari, Philip H. S. Torr, [Struck: Structured Output Tracking with Kernels](#), ICCV 2011

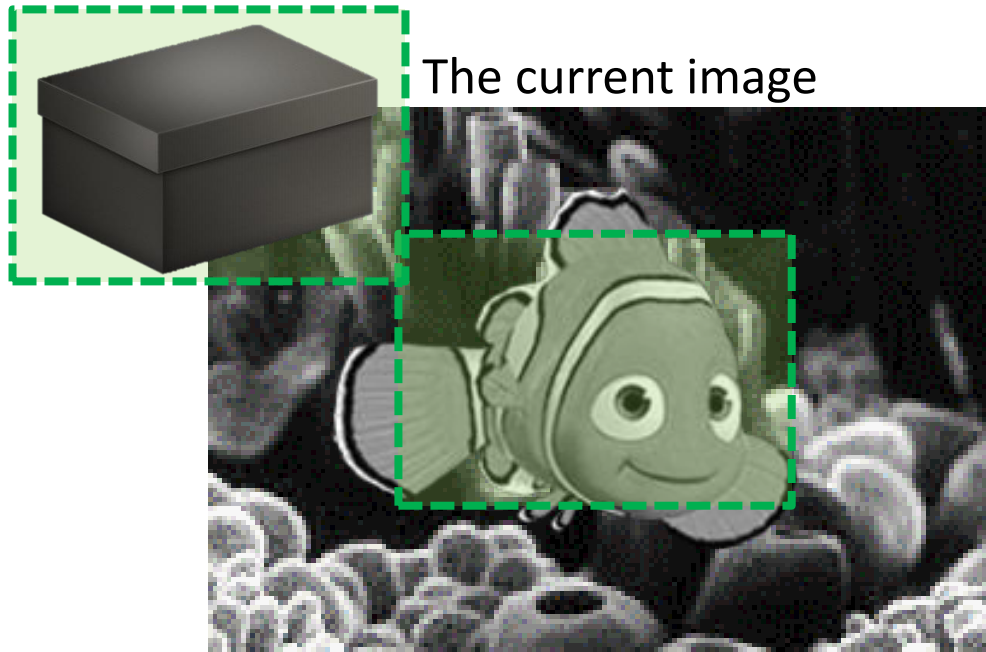
Struck tracking example



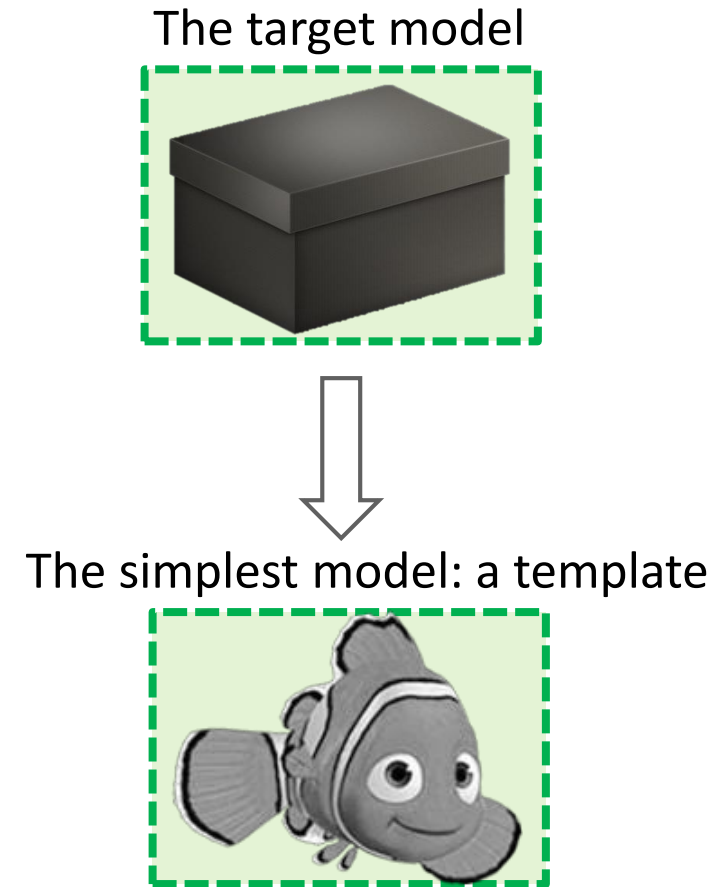
Sam Hare, Amir Saffari, Philip H. S. Torr, [Struck: Structured Output Tracking with Kernels](#), ICCV 2011

Let's take a step back...

- How is target detection carried out?

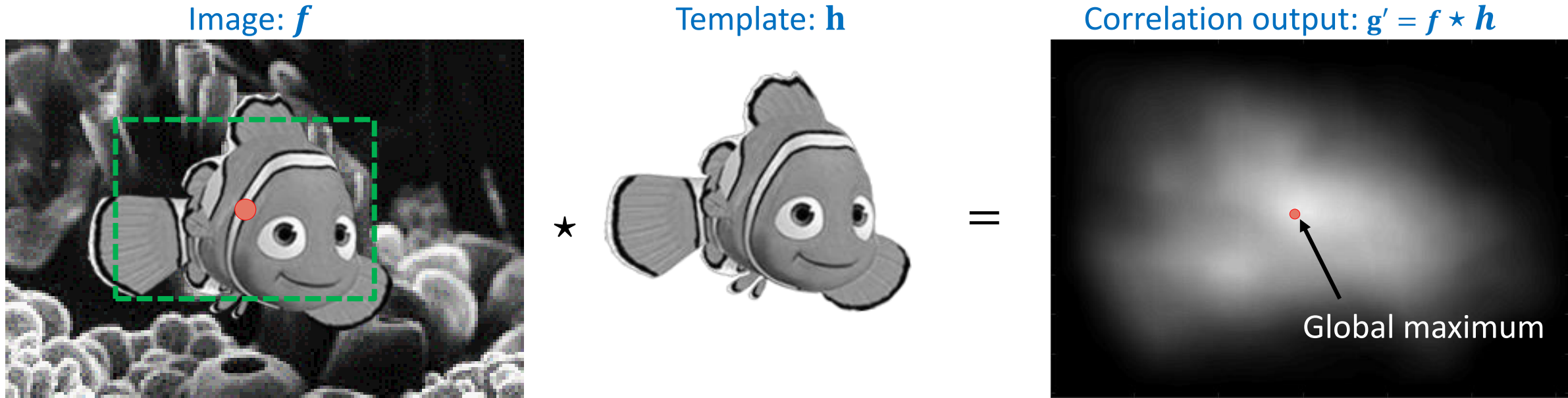


- Looks like a convolution/correlation
- A simplest model is the template



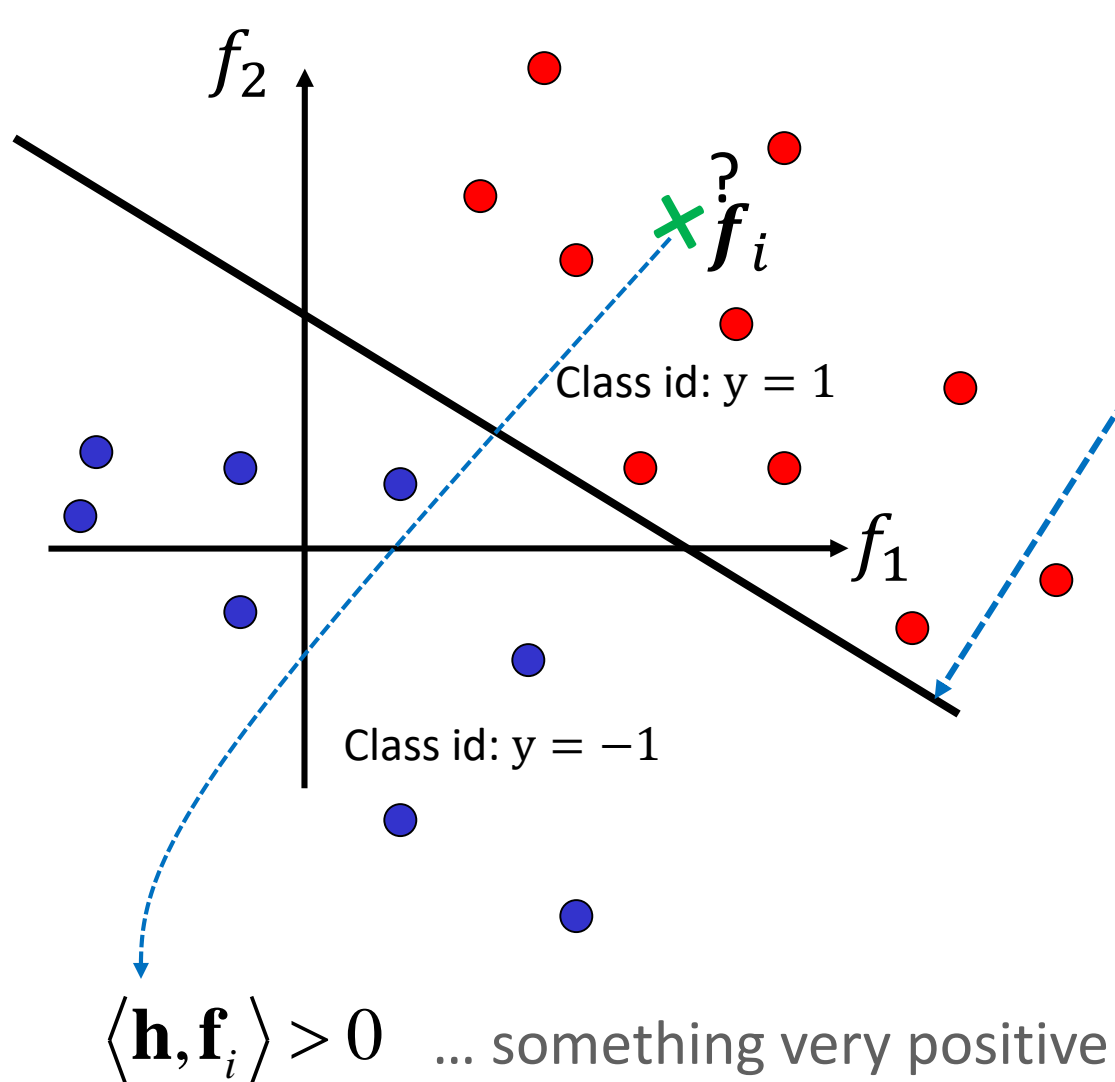
Correlation-based tracking

- Target localization: *maximum of correlation* of image f with a template h .



- Recall how correlation is computed:
 - Crop a patch from f , pointwise multiply with the template h and sum.
 - I.e., a dot product between the cropped patch and template.

Dot product implements a linear classifier / regressor



A decision boundary, in general, a *hyper-plane*:

$$af_1 + cf_2 + b = 0$$

Define:

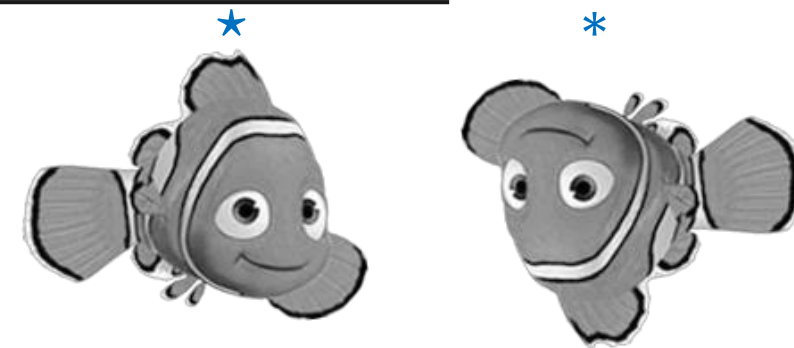
$$\mathbf{h} = \begin{bmatrix} a \\ c \\ b \end{bmatrix} \quad \mathbf{f} = \begin{bmatrix} f_1 \\ f_2 \\ 1 \end{bmatrix}$$

A general hyper-plane eq:

$$\langle \mathbf{h}, \mathbf{f} \rangle = \mathbf{h}^T \mathbf{f} = 0$$

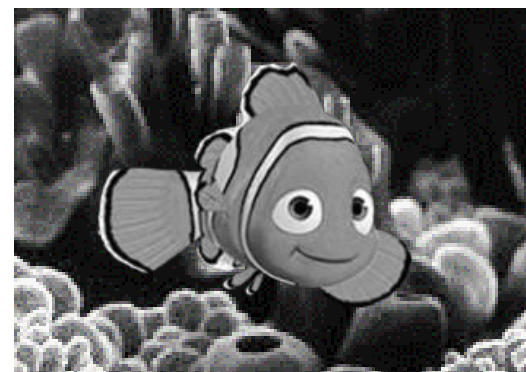
Efficient correlation computation

1. Correlation is a convolution using a flipped image:
2. Correlation equivalent to point-wise product in Fourier domain:

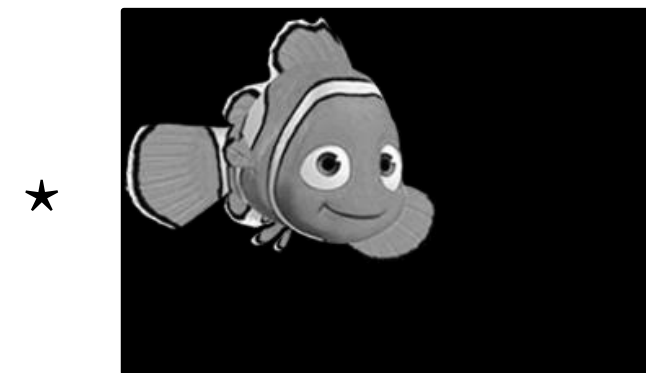


$$g = f \star h \Leftrightarrow \hat{g} = \hat{f} \odot \overline{\hat{h}}$$

- Where:
 - $\hat{g} = \mathcal{F}(g)$... Fourier transform of g .
 - \odot ... element-wise product
 - $\overline{(\cdot)}$... complex conjugate (i.e., imaginary part negated)
- Requirement:
 f and h must be of the same size

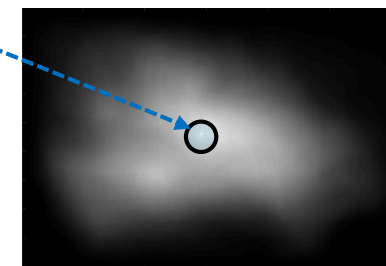
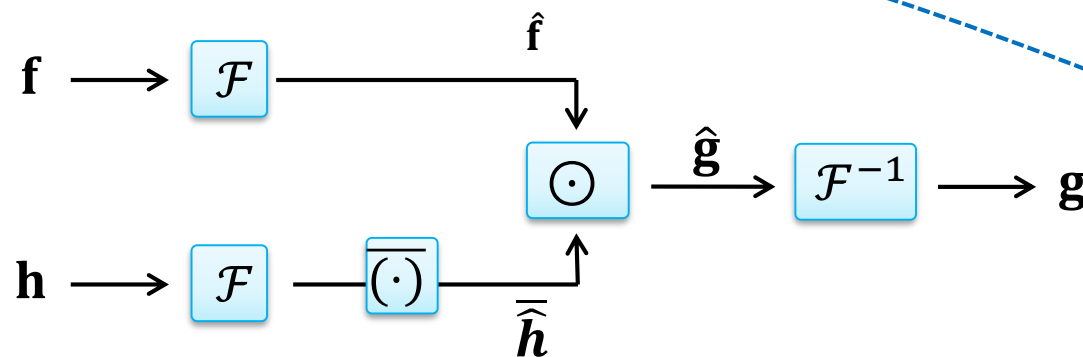
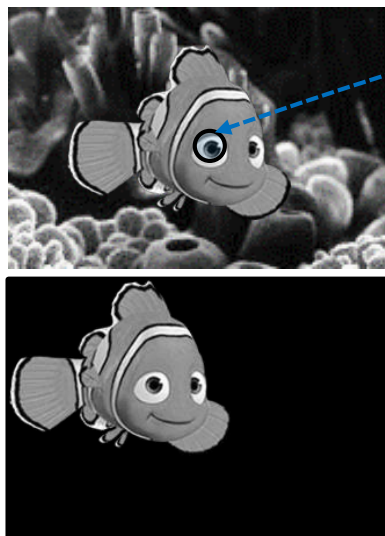


pad the template with zeros



Efficient correlation computation

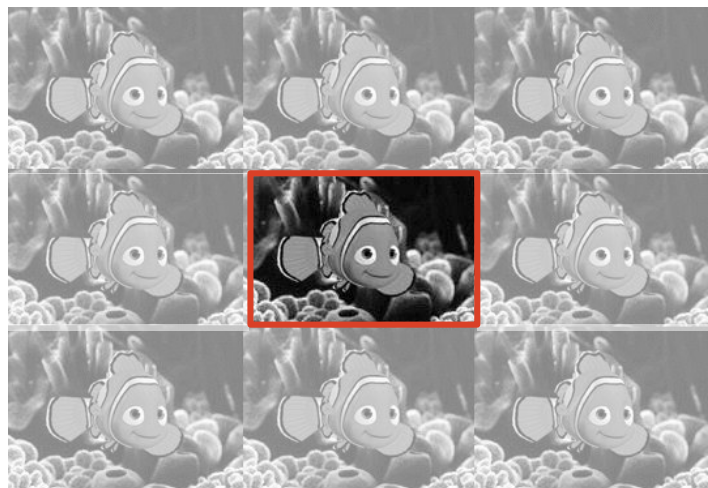
- Correlation via Fourier domain: $g = f \star h \Leftrightarrow \hat{g} = \hat{f} \odot \overline{\hat{h}}$



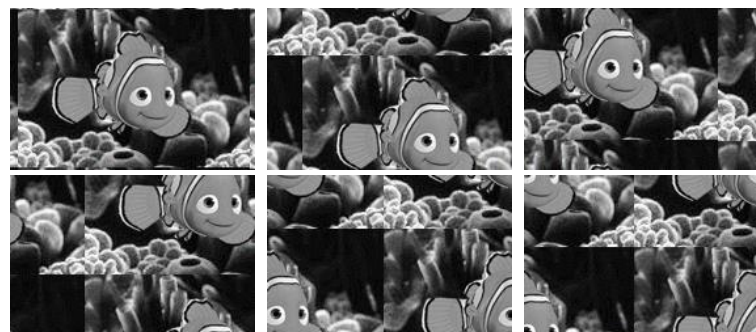
- Orders of magnitude speedup:
 - For $n \times n$ images, cross-correlation is $\mathcal{O}(n^4)$.
 - Fast Fourier Transform (and its inverse) are $\mathcal{O}(n^2 \log n)$.

Efficient correlation computation

- Correlation is *circular* in discrete Fourier transform (DFT)!



Circular shifts

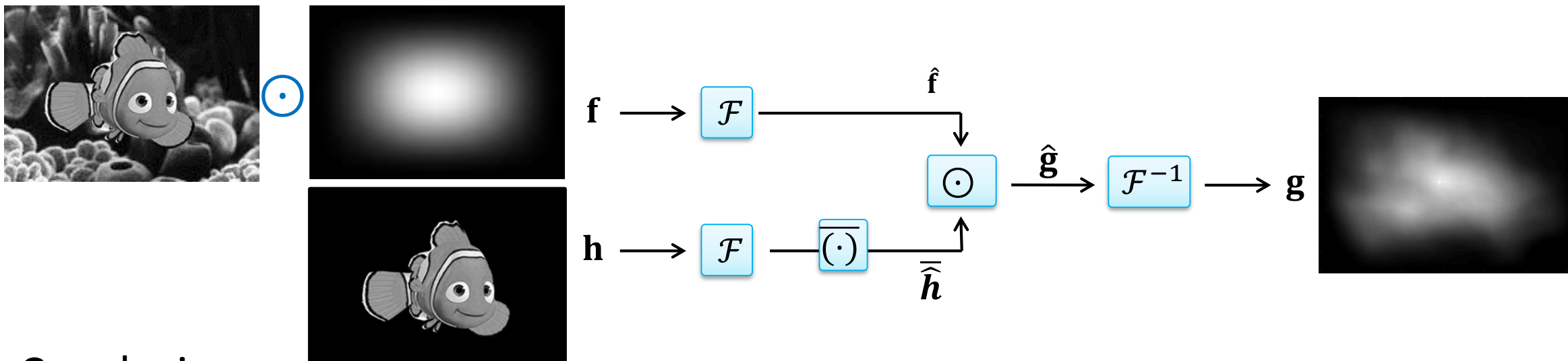


- To reduce the boundary effect, multiply the image f by a Hanning window:



Efficient correlation computation

- Correlation via Fourier domain: $g = f \star h \Leftrightarrow \hat{g} = \hat{f} \odot \overline{\hat{h}}$

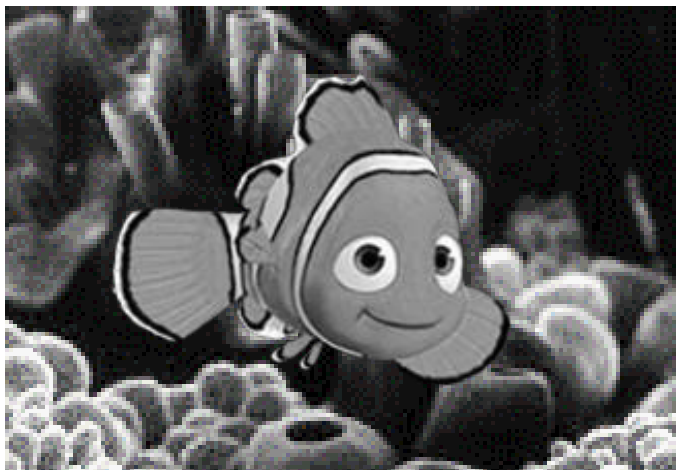


- Conclusion:
 - Correlation can be significantly accelerated by FFT
 - Since it evaluates $\langle f, h \rangle$ at all displacements it implements a fast linear classifier (regressor) evaluation at all displacements!
 - But how to learn the most suitable template h ?

Discriminative correlation learning

- Ideally, we would like a well expressed maximum at the object location:

Image: f



Template: h



Correlation output: $g' = f \star h$

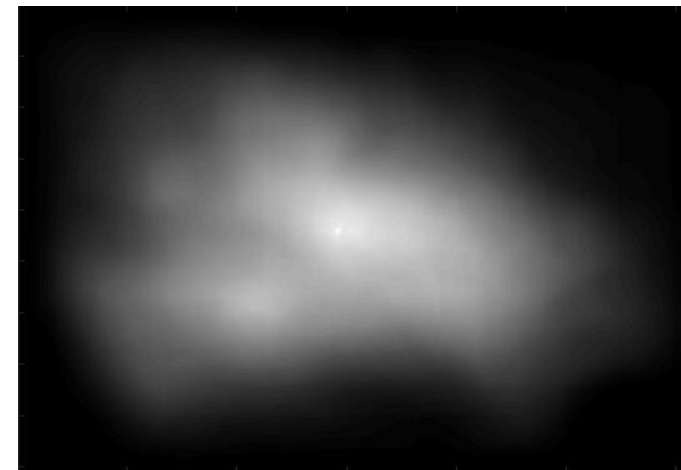
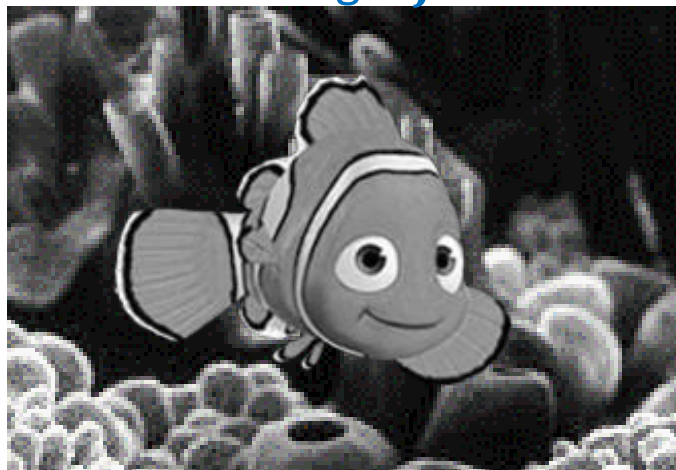
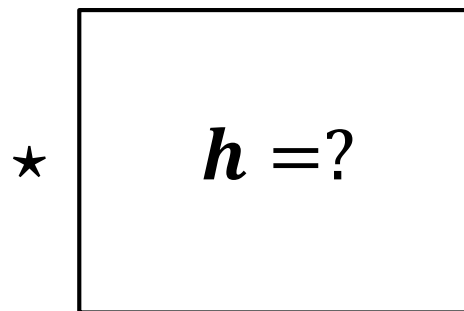


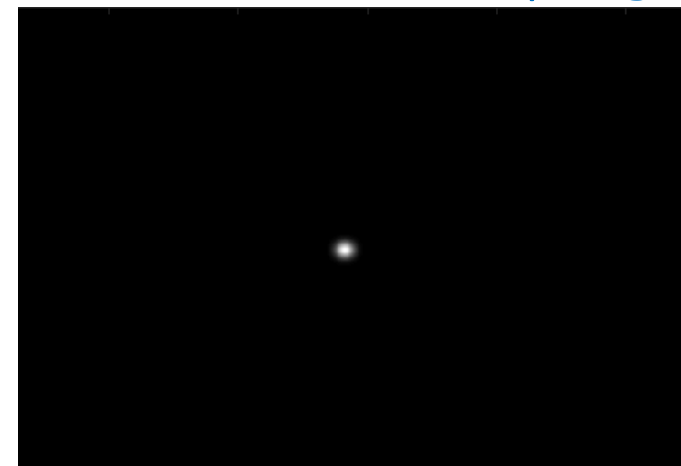
Image: f



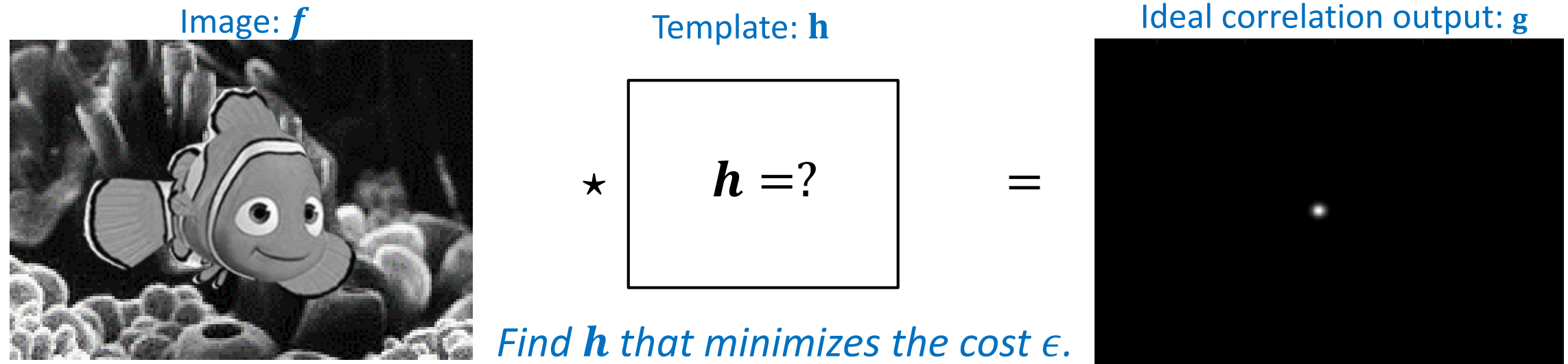
Template: h



Ideal correlation output: g



Discriminative Correlation Filters



- **Formalize the cost:** difference between the correlation of template h with the image f , i.e.,

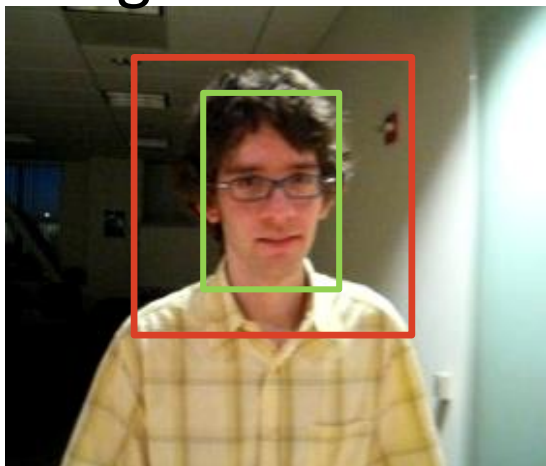
$$\epsilon = \|f \star h - g\|^2 + \lambda \|h\|^2.$$

- **Learning:** Given the image f , find the filter h that minimizes ϵ .

Discriminative Correlation Filters – maths

Discriminative Correlation Filters in a nutshell

Target localized



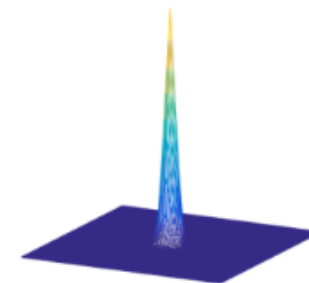
Training example: f



Template: h

\star

$=$



Desired response: g

green bbox: target region, red bbox: search region

Pixel-wise product!

$$\arg \min_{\mathbf{h}} |\mathbf{f} \star \mathbf{h} - \mathbf{g}|^2 + \lambda |\mathbf{h}|^2 = \arg \min_{\hat{\mathbf{h}}} |\hat{\mathbf{f}} \odot \bar{\hat{\mathbf{h}}} - \hat{\mathbf{g}}|^2 + \lambda |\hat{\mathbf{h}}|^2$$

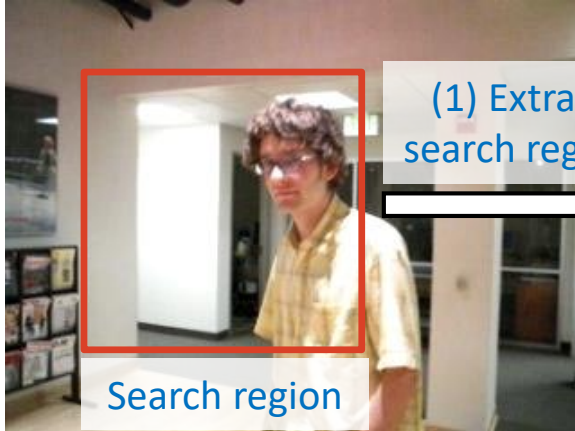
$$\text{Closed-form solution: } \bar{\hat{\mathbf{h}}} = \frac{\hat{\mathbf{g}} \odot \bar{\hat{\mathbf{f}}}}{\hat{\mathbf{f}} \odot \bar{\hat{\mathbf{f}}} + \lambda}$$

Pixel-wise division!

Tracking algorithm outline

Localization step: Filter application

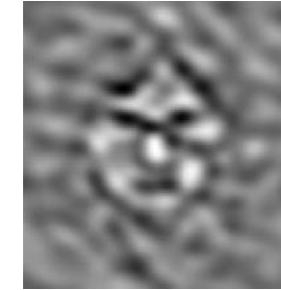
Current image



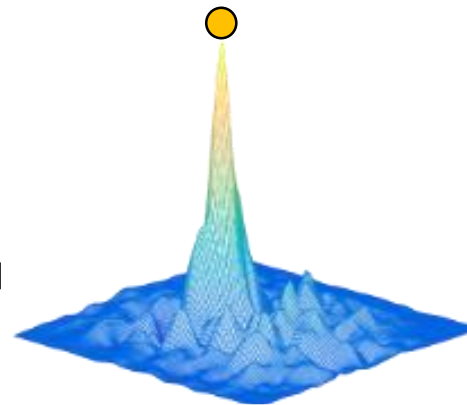
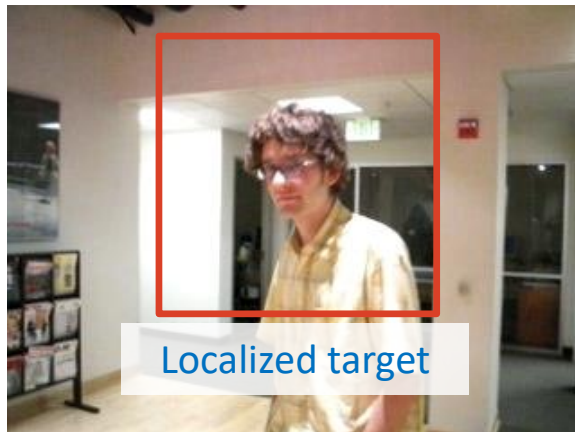
(2) Compute FFT of the modified search region



Filter: h, \hat{h}



$$(\cdot)^\dagger = (\bar{\cdot})$$



(4) Take max position as target center

$$IFFT(\hat{f} \odot \hat{h}^\dagger)$$

(3) Multiply region and template and inverse FFT

Tracking algorithm outline

Update step: Filter learning

Current image



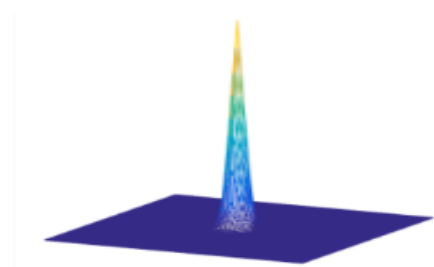
(1) Extract region

(2) Compute FFT of the modified region



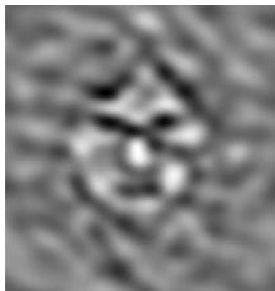
$$FFT(\text{Localized target} \odot \text{Mask}) = \hat{\mathbf{f}}$$

(3) Compute FFT of desired response $\hat{\mathbf{g}} = FFT(g)$



$$(\cdot)^\dagger = (\bar{\cdot})$$

Final filter: $\mathbf{h}, \hat{\mathbf{h}}$



$$\hat{\mathbf{h}}_k = \hat{\mathbf{h}}_{k-1} \alpha + \hat{\mathbf{h}} (1 - \alpha)$$

(5) Average the filter with filter from previous time-step

$$\hat{\mathbf{h}}^\dagger = \frac{\hat{\mathbf{g}} \odot \hat{\mathbf{f}}^\dagger}{\hat{\mathbf{f}} \odot \hat{\mathbf{f}}^\dagger}$$

(4) Compute the filter

A basic CF tracker: MOSSE

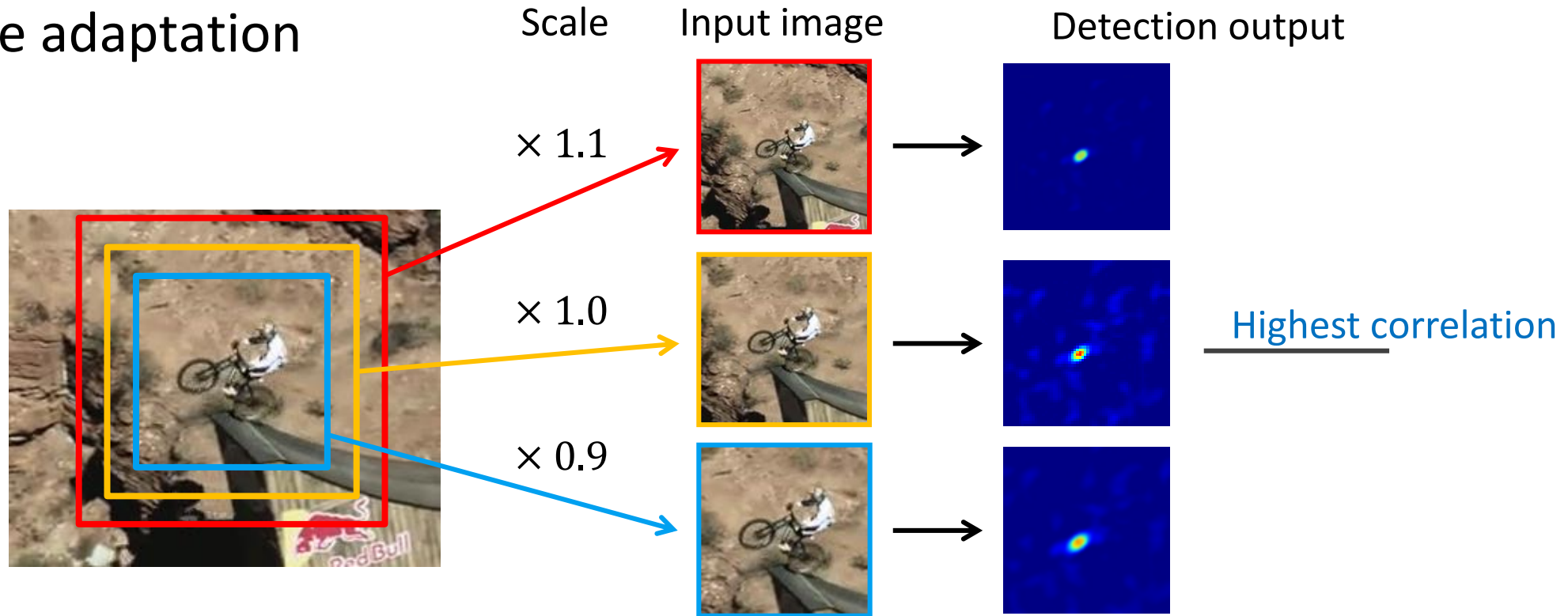


Simplest version reaches speeds approximately 300fps.

Bolme, Beveridge, Draper, Lui, Visual Object Tracking using Adaptive Correlation Filters, CVPR2010

Scale estimation during tracking

- Scale adaptation

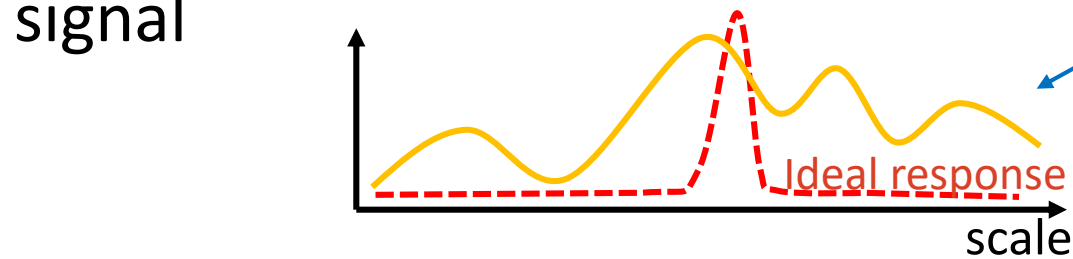


- Extract patches with **different scales** and normalize them to the **same size**
- Run classification (correlation) on all patches and output bounding box with the **highest response**

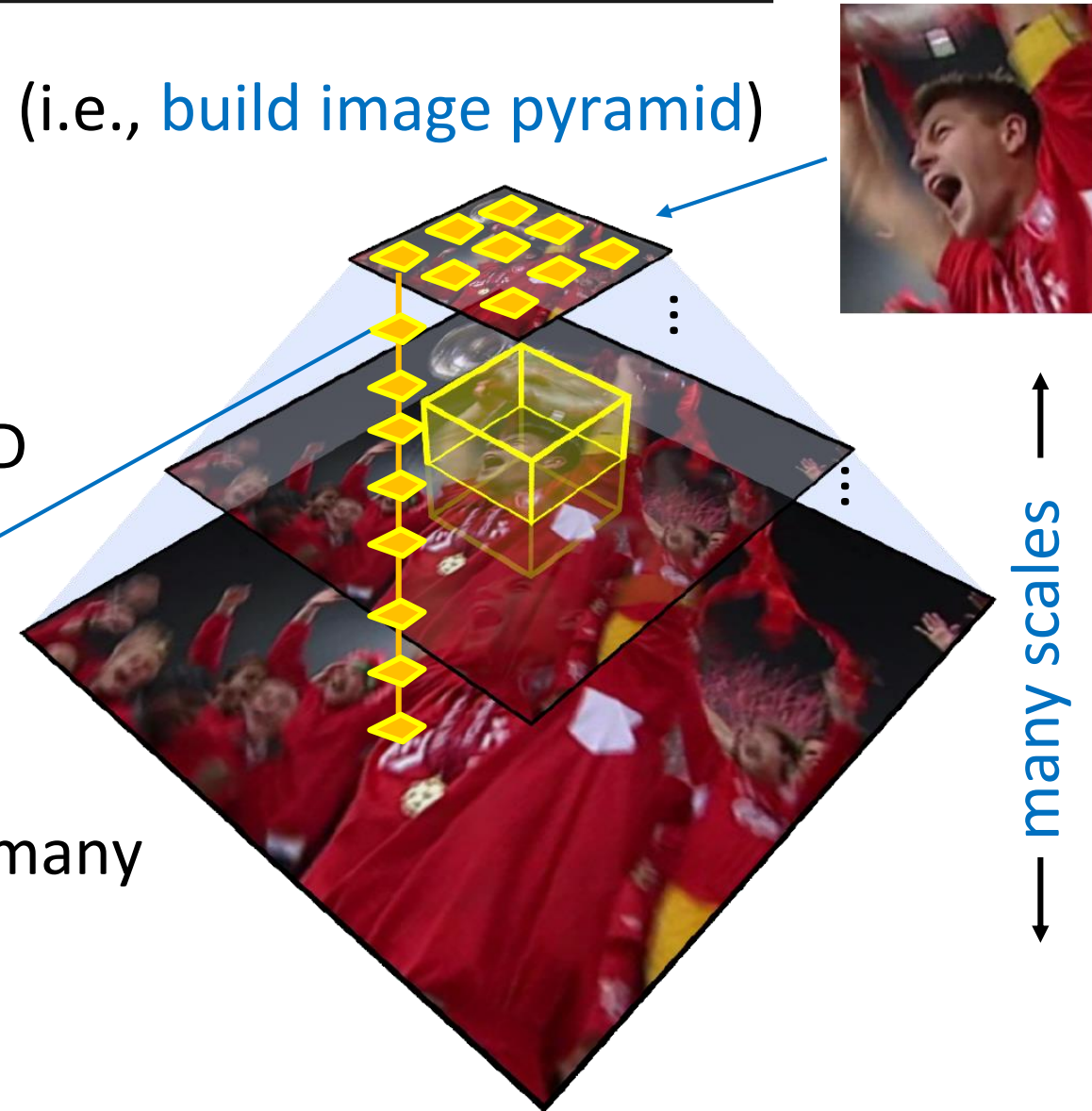
Scale estimation by DCF: Learning

- Resize the image patch to various sizes (i.e., **build image pyramid**)
- Take image intensities **along each pixel** through the scale-space.

- **Learn a correlation filter \mathbf{h}_1** over the 1D signal

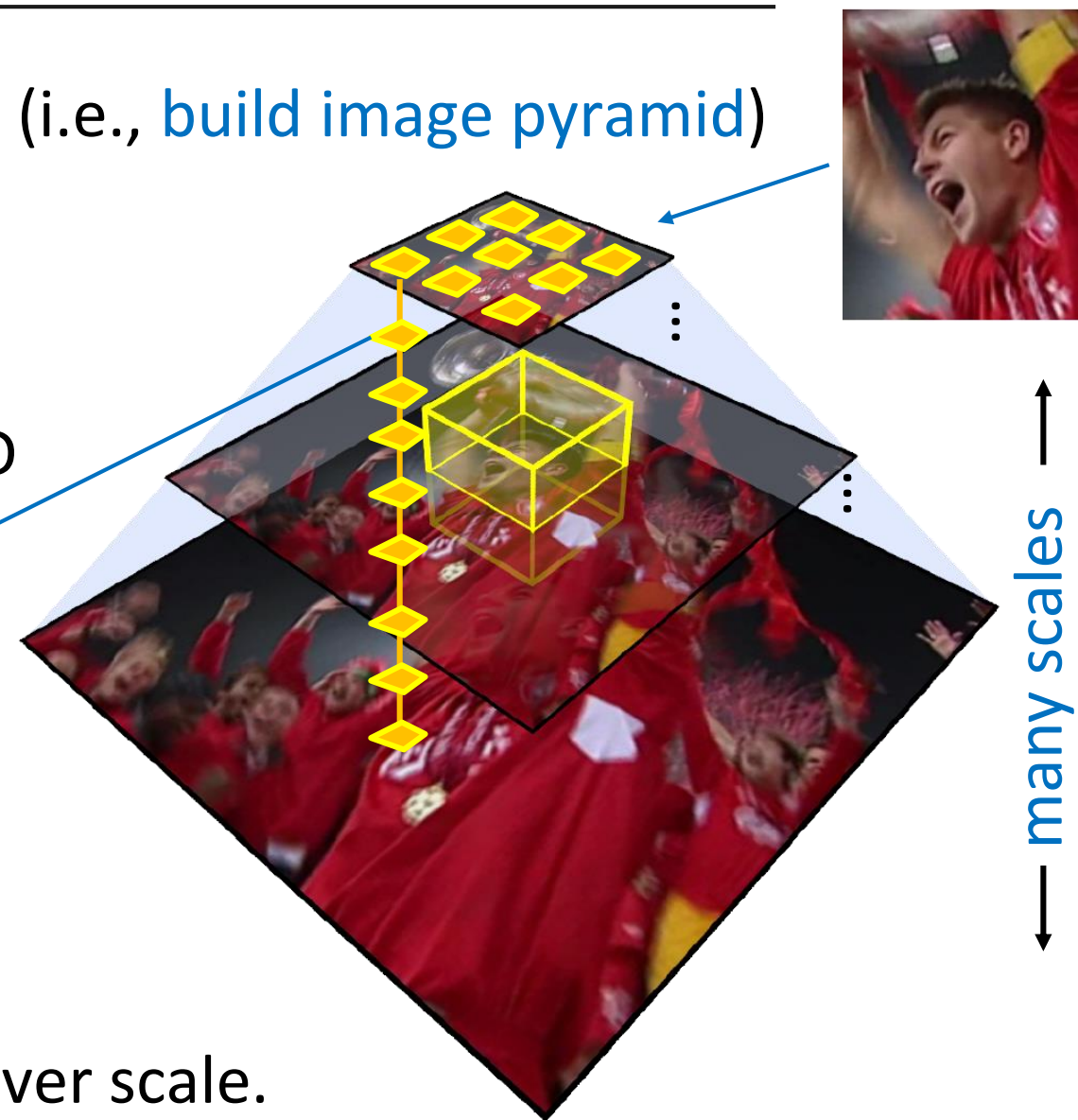
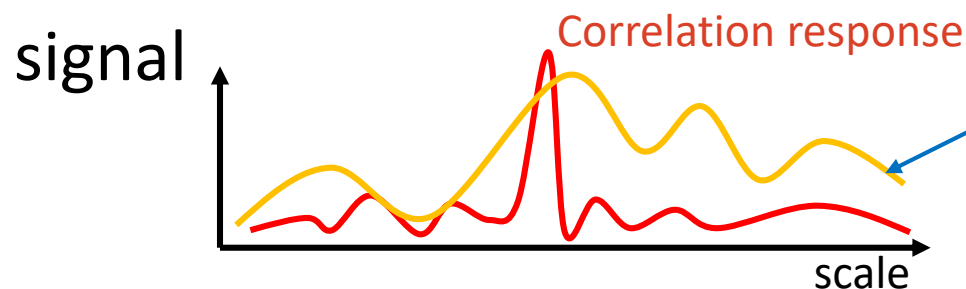


- Repeat this for all N pixels and obtain many 1D correlation filters $\{\mathbf{h}_i\}_{i=1:N}$.
- Multichannel version proposed in [1]



Scale estimation by DCF: Estimation

- Resize the image patch to various sizes (i.e., build image pyramid)
- Take image intensities along each pixel through the scale-space.
- Apply the corresponding filter h_i on 1D signal
- Repeat for all 1D signals at other N locations.
- Average the responses, take the max over scale.



Scale estimation by DCF

1. Localize (standard DCF)
2. Estimate scale (scale DCF)

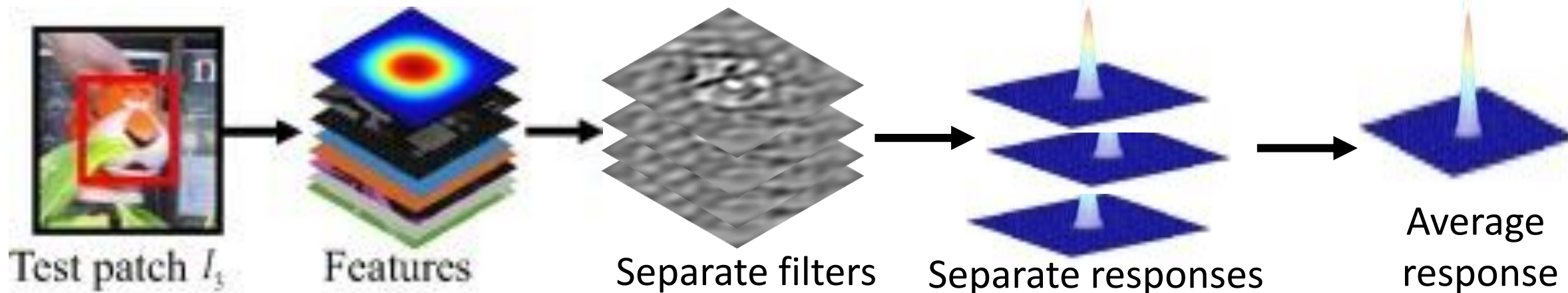


Danelljan, M., Hager, G., Khan, F.S., Felsberg, M.: [Accurate scale estimation for robust visual tracking](#). BMVC2014

Multichannel formulations

Multichannel formulation

- Henriques et al. – KCF (HoG 31-multi-channel features)



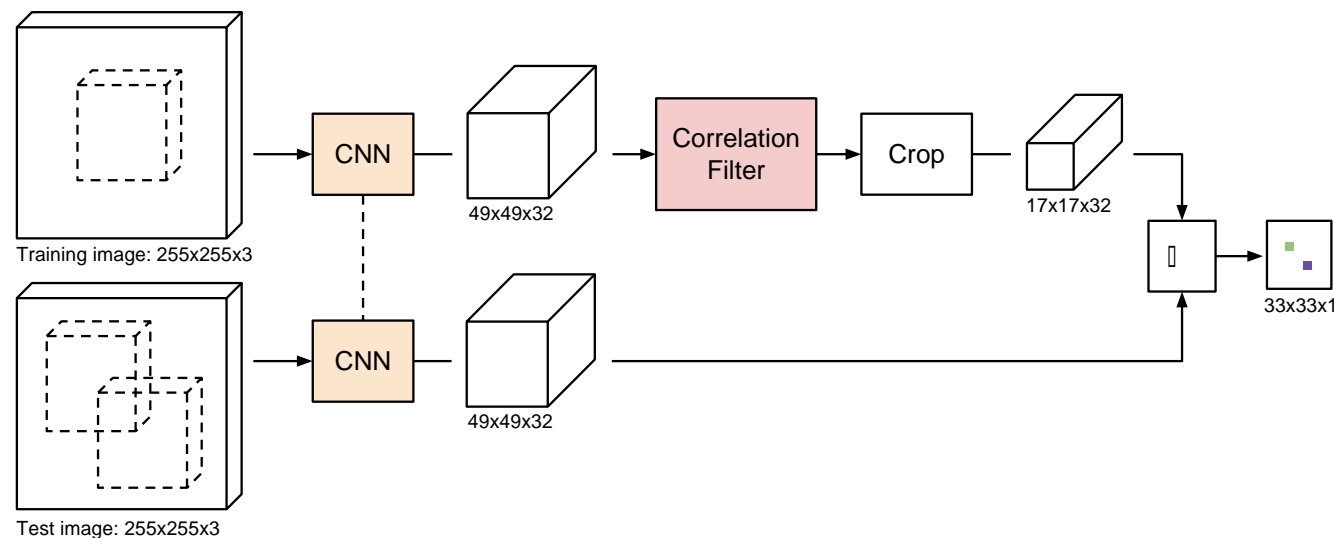
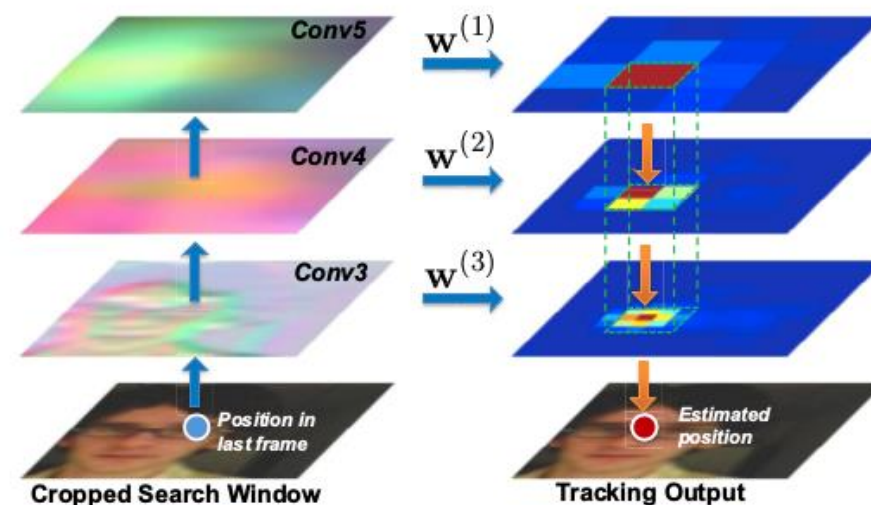
Further work

- Li et al. A Scale Adaptive Kernel Correlation Filter Tracker with Feature Integration, ECCVW2014:
 - HoG (31), color-naming (11 dimensional color representation) and grayscale pixels features
 - Quantize scale space and normalize each scale to a single (common) size by bilinear interpolation
→ only one filter on normalized size

Better channel features

CNN-based Correlation Trackers

- Bhat et al. (ECCV 2018)
 - Goutam Bhat et al. "Unveiling the Power of Deep Tracking", ECCV 2018.
 - features: VGG-Net pretrained on ImageNet dataset extracted from several layers
 - Fusion of different feature channels into a single response
- Valmadre et al. (CVPR 2017)
 - Learn CNN features for DCF

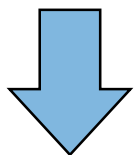
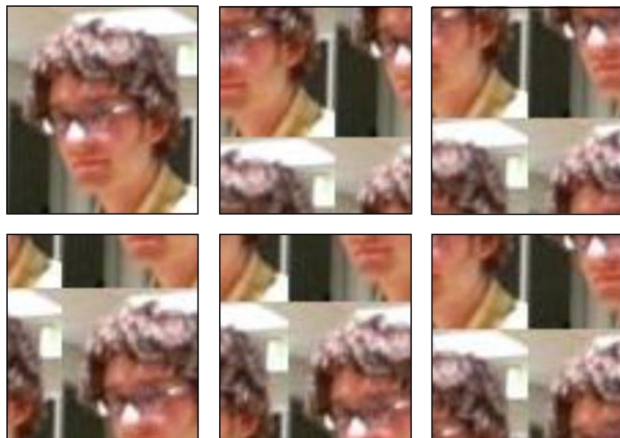


Pictures were obtained from authors publication:

- Chao Ma, Jia-Bin Huang, Xiaokang Yang, and Ming-Hsuan Yang, "Hierarchical Convolutional Features for Visual Tracking," International Conference on Computer Vision (ICCV), 2015.
- Valmadre, Bertinetto, Henriques, Vedaldi, Torr, End-to-end representation learning for Correlation Filter based tracking, CVPR2017

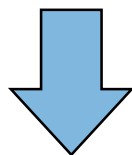
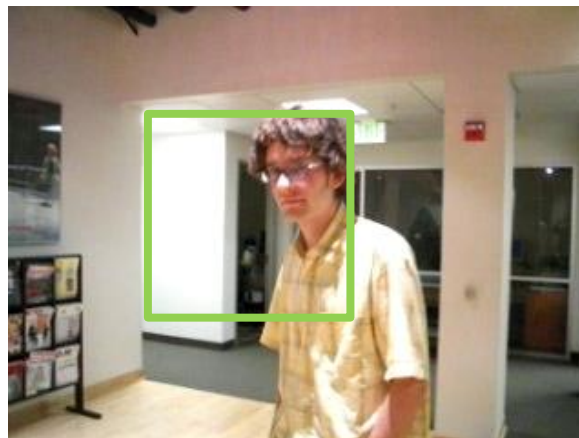
Issues with standard DCFs: search region

Filter learned from
cyclic shifts



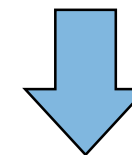
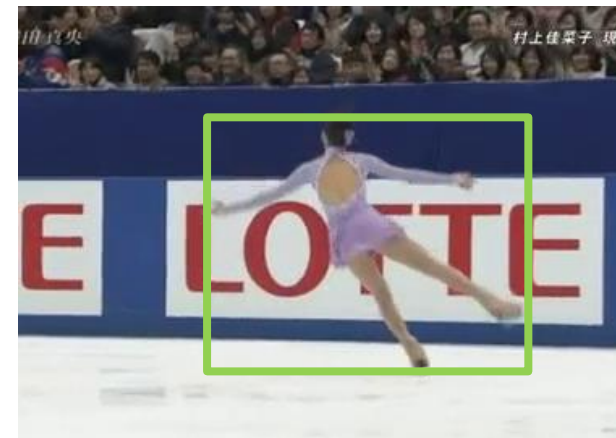
Unrealistic
training
examples

Search region size
equal to filter size



Difficult to address
large displacements

Poor approximation
with bbox



Background
enters filter

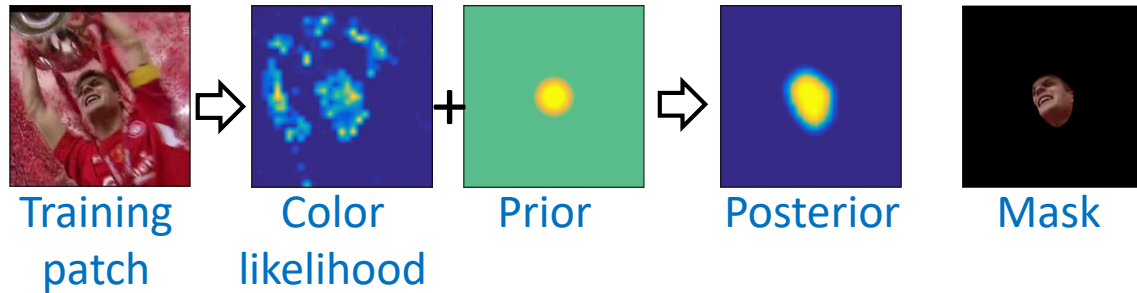
CSRDCF: Constrained filter learning

- Discriminative Correlation Filter with Channel and Spatial Reliability
Lukežič, Čehovin, Vojir, Matas, Kristan, Discriminative Correlation Filter with Channel and Spatial Reliability, CVPR2017 (extended/updated version IJCV2019)
- State-of-the-art results, **outperformed** even **trackers based on CNN**
- **Simple features:**
 - HoG features (18 contrast sensitive orientation channels)
 - binarized grayscale channel (1 channel)
 - color names (~mapping of RGB to 10 channels)
- **Single-CPU** single-thread, Matlab implementation @13 fps, C++ realtime ; part of OpenCV

CSRDCF outline

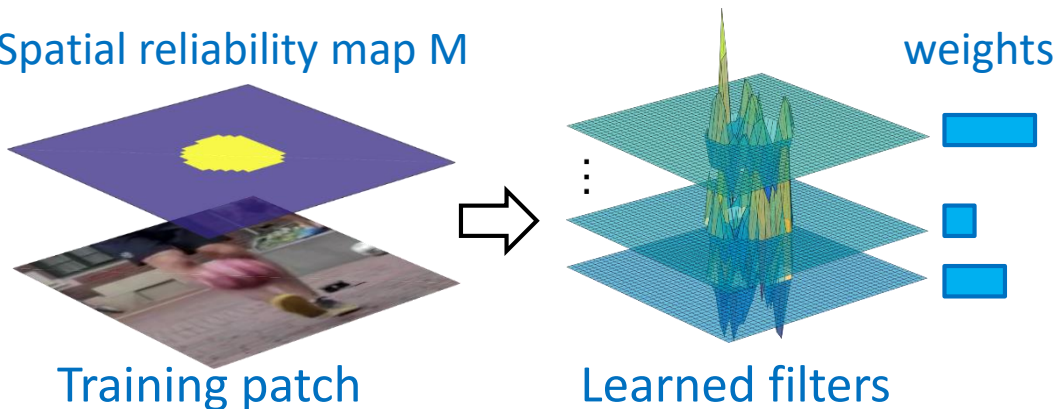
Training:

- Estimate object segmentation \rightarrow object mask



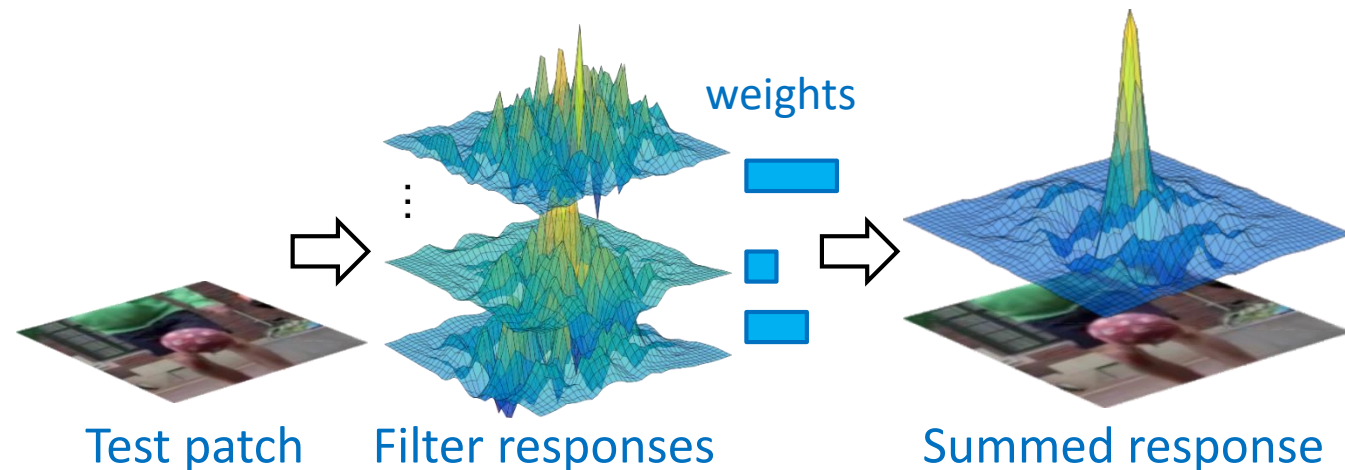
- Learn correlation filter using the object mask as constraints
- Estimate weights of the feature channels

Spatial reliability map M



Localization:

- Compute response map from the weighted feature channels responses
- Estimate best position
- Estimate scale (standard approach in correlation tracking)



CSRDCF computational challenges

- The cost function becomes complicated when filter masking is considered

$$\epsilon = \|\hat{\mathbf{f}} \odot \hat{\mathbf{h}} - \hat{\mathbf{g}}\|^2 + \lambda \|\hat{\mathbf{h}}\|^2 ; \mathbf{h} = \mathbf{h} \odot \mathbf{m}$$

- A closed-form solution does not exist, but the problem can be reformulated and solved by Alternate Direction Method of Multipliers (ADMM).

See these papers for a practical example of ADMM uses:

(full derivation in the appendix of [1])

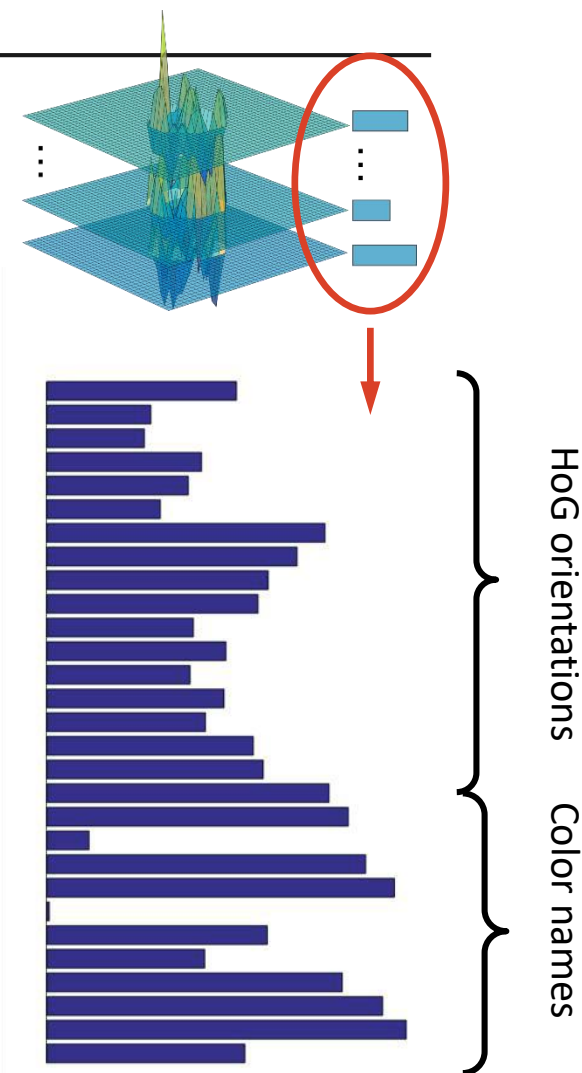
[1] Lukežič, Čehovin, Vojir, Matas, Kristan, [Discriminative Correlation Filter with Channel and Spatial Reliability](#), CVPR2017 (extended/updated version IJCV2019)

[2] Lukežič, Čehovin Zajc, Kristan, [Fast Spatially Regularized Correlation Filter Tracker](#), ERK 2018

CSRDCF – example



Tracking result



Channel reliability weights

CSRDCF – segmentation mask

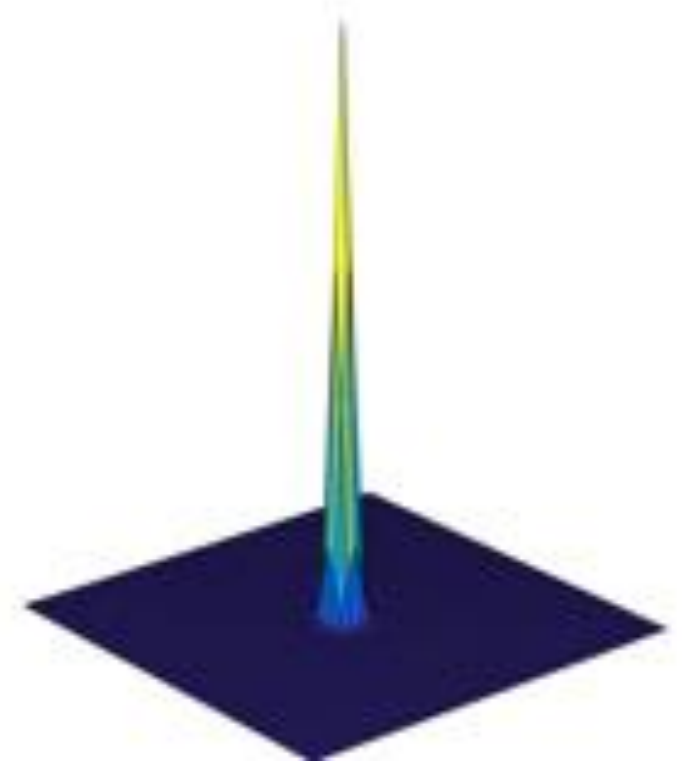


Lukežič, Vojříř, Čehovin, Matas, Kristan, *Discriminative Correlation Filter with Channel and Spatial Reliability*, CVPR 2017.

CSRDCF – nonrigid target



Input image



CF response

Lukežič, Vojíř, Čehovin, Matas, Kristan, *Discriminative Correlation Filter with Channel and Spatial Reliability*, CVPR 2017.

Applications: AR.Drone [1]



Alan Lukežič, Jon Natanael Muhovič, Tina Strgar

[1] M. Kristan, Računalniški vid v avtonomnih robotskih sistemih, Noč raziskovalcev (Ljubljana, September 2015)

Alternative constrained filter learning approaches

- Constrained filter learning has been explored before:
 - [1] Danelljan, Häger, Khan, Felsberg, Learning Spatially Regularized Correlation Filters for Visual Tracking. ICCV 2015
 - [2] Hamed Kiani Galoogahi, Terence Sim, Simon Lucey, Correlation Filters with Limited Boundaries. CVPR 2015
- A followup continuous formulation:
 - [3] Martin Danelljan, Goutam Bhat, Fahad Khan, Michael Felsberg, ECO: Efficient Convolution Operators for Tracking, CVPR 2017

Discriminative tracking – summary

- Optimization technique:
various, **some in closed form**, some as efficient variants of **gradient descent**
- Cost functions:
Discriminative – foreground/background differentiability maximized!
- Attractive properties:
 - **Potentially fast** learning and fast application (e.g., ~300fps MOSE)
 - **Performance may be boosted** in straight-forward manner by better features.
 - **Further boosts** by *learning* the best features for tracking

References

- Online Adaboost for tracking:
 - H. Grabner et. al., Real-Time Tracking via On-line Boosting . BMVC, 2006.
- Multiple instance learning for tracking:
 - Babenko et al., "[Robust Object Tracking with Online Multiple Instance Learning](#)", TPAMI2011
- Structured SVM tracking:
 - Hare, Saffari, Torr, Struck: Structured Output Tracking with Kernels, ICCV 2011
- Correlation filter tracking:
 - Bolme, Beveridge, Draper, and Y. M. Lui. Visual Object Tracking using Adaptive Correlation Filters, CVPR 2010.
 - Henriques, Caseiro, Martins, Batista, High-Speed Tracking with Kernelized Correlation Filters, TPAMI2015
 - Danelljan, M., Hager, G., Khan, F.S., Felsberg, M.: Accurate scale estimation for robust visual tracking, BMVC2014
 - Danelljan, Häger, Khan, Felsberg, Learning Spatially Regularized Correlation Filters for Visual Tracking. ICCV 2015
 - Lukežič, Vojíř, Čehovin, Matas, Kristan, *Discriminative Correlation Filter with Channel and Spatial Reliability*, CVPR 2017
 - Chao Ma, Jia-Bin Huang, Xiaokang Yang, and Ming-Hsuan Yang, Hierarchical Convolutional Features for Visual Tracking, ICCV 2015
 - Valmadre, et al., End-To-End Representation Learning for Correlation Filter Based Tracking, CVPR2017